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6.094 Introduction to MATLAB®  
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**6.094**

Introduction to Programming in MATLAB®

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**Lecture 2: Visualization and Programming**

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IAP 2009

# Outline

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**(1) Plotting Continued**

(2) Scripts

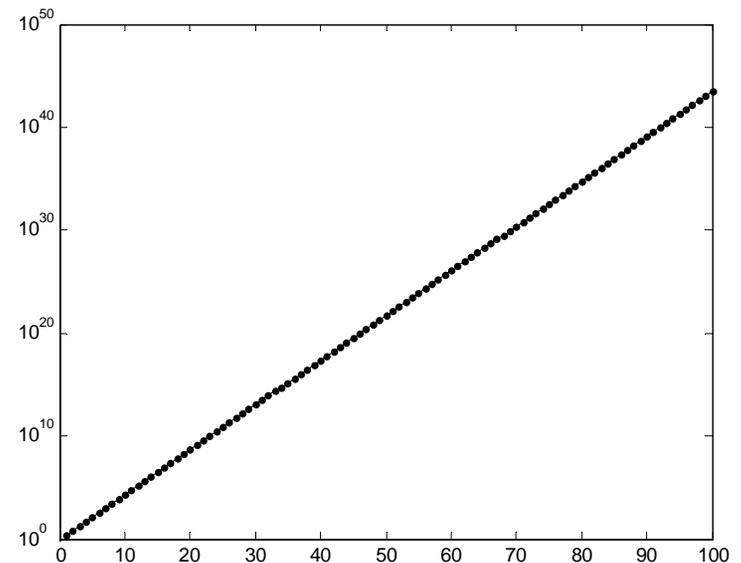
(3) Functions

(4) Flow Control

# Cartesian Plots

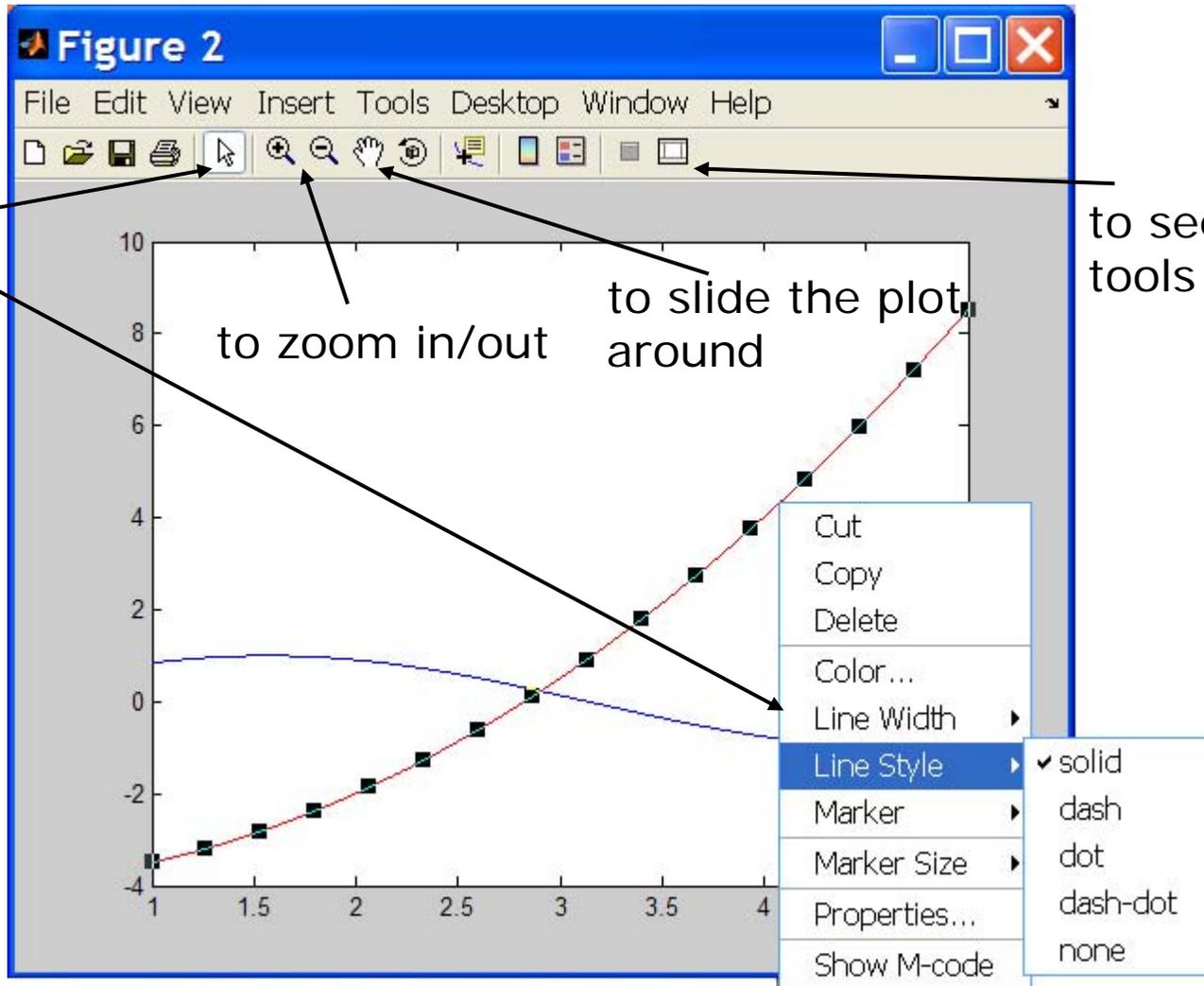
---

- We have already seen the plot function
  - » `x=-pi:pi/100:pi;`
  - » `y=cos(4*x).*sin(10*x).*exp(-abs(x));`
  - » `plot(x,y,'k-');`
- The same syntax applies for semilog and loglog plots
  - » `semilogx(x,y,'k');`
  - » `semilogy(y,'r.-');`
  - » `loglog(x,y);`
- For example:
  - » `x=0:100;`
  - » `semilogy(x,exp(x),'k.-');`



# Playing with the Plot

to select lines  
and delete or  
change  
properties

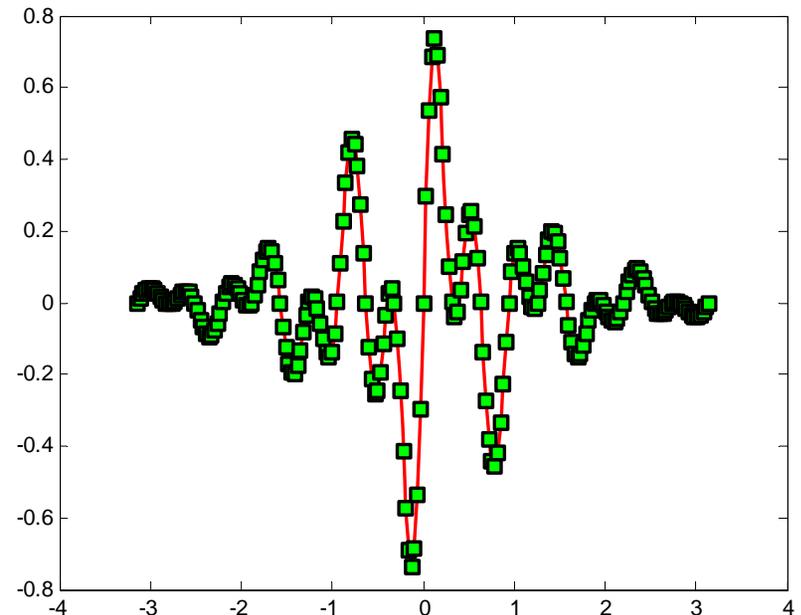


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# Line and Marker Options

- Everything on a line can be customized
  - » `plot(x,y,'--rs','LineWidth',2,...`  
`'MarkerEdgeColor','k',...`  
`'MarkerFaceColor','g',...`  
`'MarkerSize',10)`

- See [doc line](#) for a full list of properties that can be specified



# Labels

---

- Last time we saw how to add titles and labels using the GUI. Can also do it command-line:
  - » `title('Stress-Strain');`
  - » `xlabel('Force (N)');`
- For multiple lines, add a legend entry for each line
  - » `legend('Steel','Aluminum','Tungsten');`
- Can specify font and size for the text
  - » `ylabel('Distance (m)','FontSize',14,...`  
`'FontName','Helvetica');`
    - use ... to break long commands across multiple lines
- To put parameter values into labels, need to use `num2str` and concatenate:
  - » `str = ['Strength of ' num2str(d) 'cm diameter rod'];`
  - » `title(str)`

# Axis

---

- A grid makes it easier to read values
  - » `grid on`
- `xlim` sets only the x axis limits
  - » `xlim([-pi pi]);`
- `ylim` sets only the y axis limits
  - » `ylim([-1 1]);`
- To specify both at once, use `axis`:
  - » `axis([-pi pi -1 1]);`
    - sets the x axis limits between -pi and pi and the y axis limits between -1 and 1
- Can specify tickmarks
  - » `set(gca, 'XTick', linspace(-pi, pi, 3))`
    - see `doc axes` for a list of properties you can set this way
    - more on advanced figure customization in lecture 4

# Axis Modes

---

- Built-in axis modes
  - » **axis square**
    - makes the current axis look like a box
  - » **axis tight**
    - fits axes to data
  - » **axis equal**
    - makes x and y scales the same
  - » **axis xy**
    - puts the origin in the bottom left corner (default)
  - » **axis ij**
    - puts the origin in the top left corner (for viewing matrices)

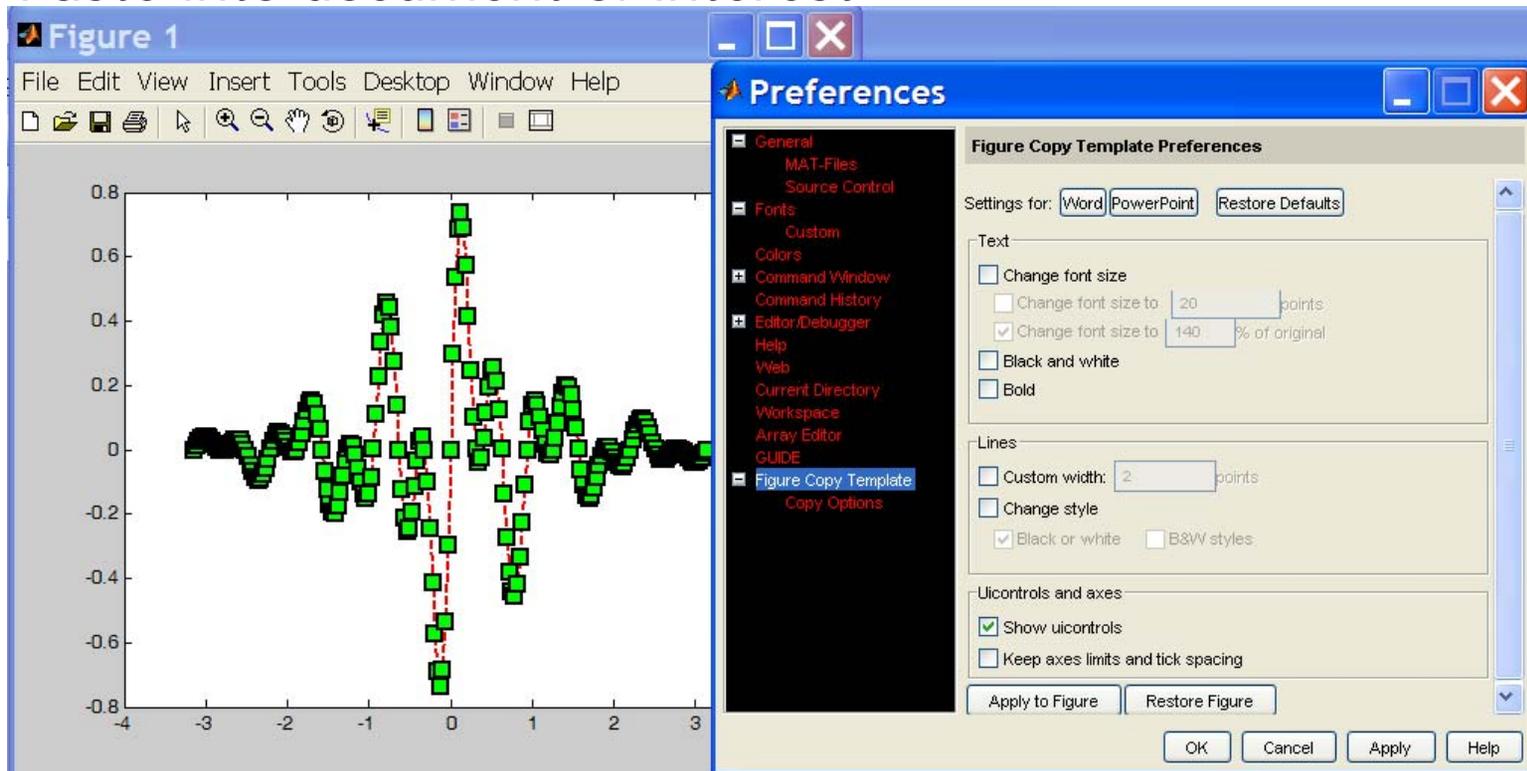
# Multiple Plots in one Figure

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- Use the figure command to open a new figure
  - » `figure`
- or activate an open figure
  - » `figure(1)`
- To have multiple axes in one figure
  - » `subplot(2,3,1)` or `subplot(231)`
    - makes a figure with 2 rows and three columns of axes, and activates the first axis for plotting
    - each axis can have labels, a legend, and a title
  - » `subplot(2,3,4:6)`
    - activating a range of axes fuses them into one
- To close existing figures
  - » `close([1 3])`
    - closes figures 1 and 3
  - » `close all`
    - closes all figures (useful in scripts/functions)

# Copy/Paste Figures

- Figures can be pasted into other apps (word, ppt, etc)
- *Edit* → *copy options* → *figure copy template*
  - Change font sizes, line properties; presets for word and ppt
- *Edit* → *copy figure* to copy figure
- Paste into document of interest



# Saving Figures

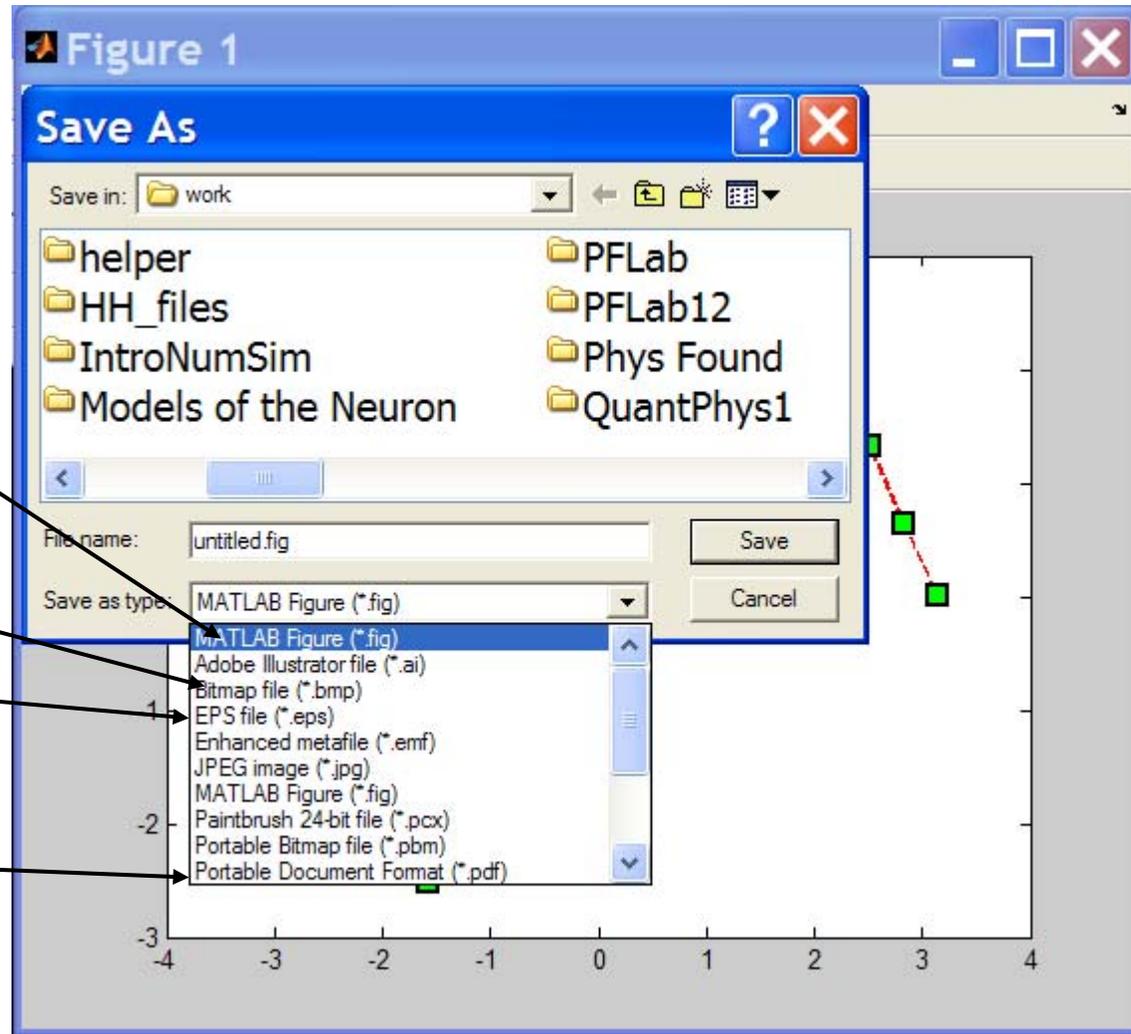
- Figures can be saved in many formats. The common ones are:

**.fig** preserves all information

**.bmp** uncompressed image

**.eps** high-quality scaleable format

**.pdf** compressed image



# Figures: Exercise

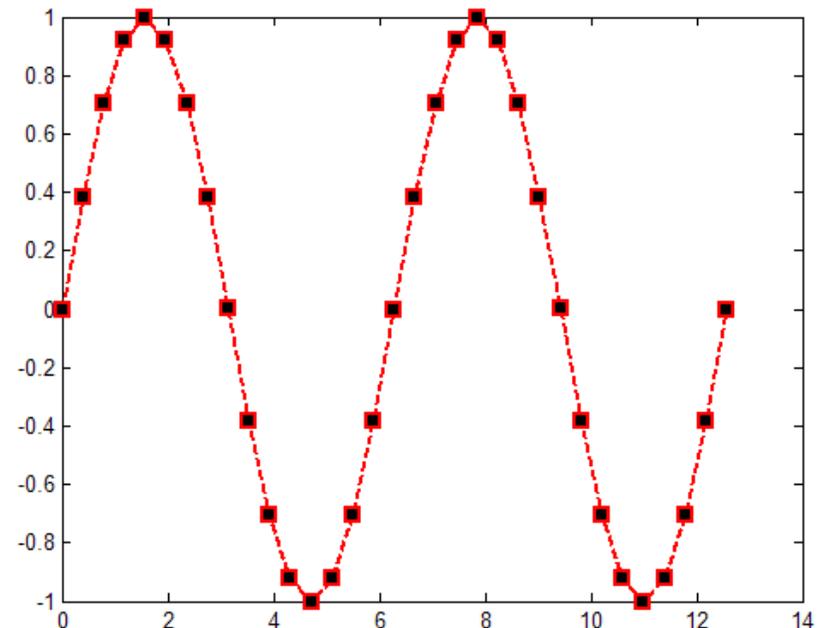
---

- Open a figure and plot a sine wave over two periods with data points at  $0, \pi/8, 2\pi/8, \dots$ . Use black squares as markers and a dashed red line of thickness 2 as the line

» `figure`

» `plot(0:pi/4:4*pi, sin(0:pi/4:4*pi), 'rs--', ...  
'LineWidth', 2, 'MarkerFaceColor', 'k');`

- Save the figure as a pdf
- View with pdf viewer.



# Visualizing matrices

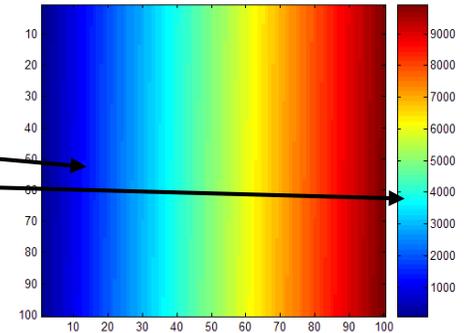
---

- Any matrix can be visualized as an image

- » `mat=reshape(1:10000,100,100);`

- » `imagesc(mat);`

- » `colorbar`



- **imagesc** automatically scales the values to span the entire colormap
- Can set limits for the color axis (analogous to `xlim`, `ylim`)
  - » `caxis([3000 7000])`

# Colormaps

- You can change the colormap:

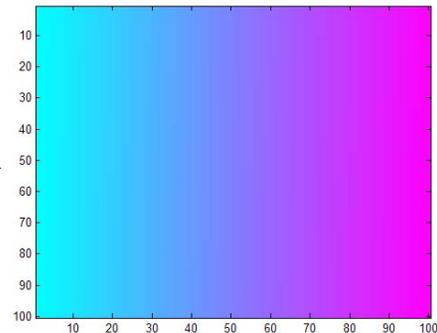
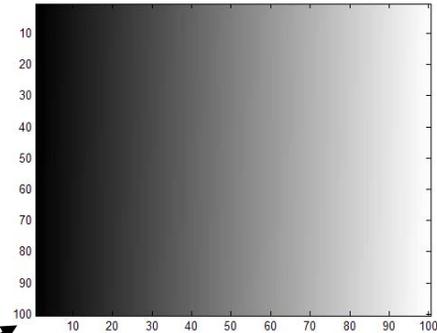
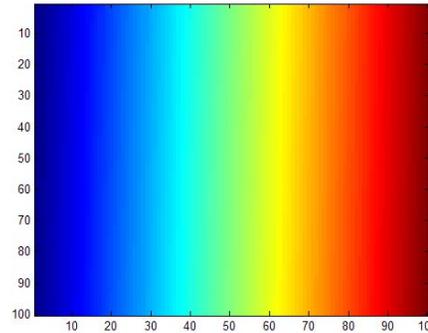
- » `imagesc(mat)`

- default map is `jet`

- » `colormap(gray)`

- » `colormap(cool)`

- » `colormap(hot(256))`



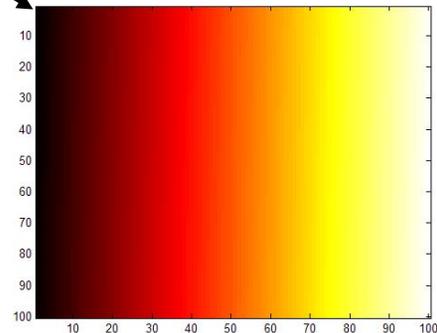
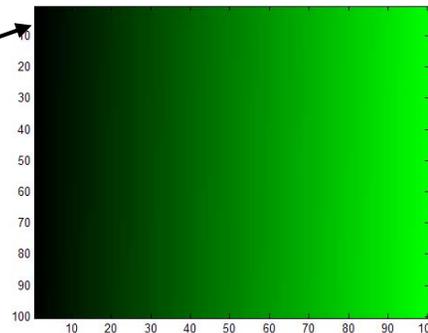
- See `help hot` for a list

- Can define custom colormap

- » `map=zeros(256,3);`

- » `map(:,2)=(0:255)/255;`

- » `colormap(map);`



# Images: Exercise

---

- Construct a Discrete Fourier Transform Matrix of size 128 using **dftmtx**
- Display the phase of this matrix as an image using a hot colormap with 256 colors

```
» dMat=dftmtx(128);  
» phase=angle(dMat);  
» imagesc(phase);  
» colormap(hot(256));
```

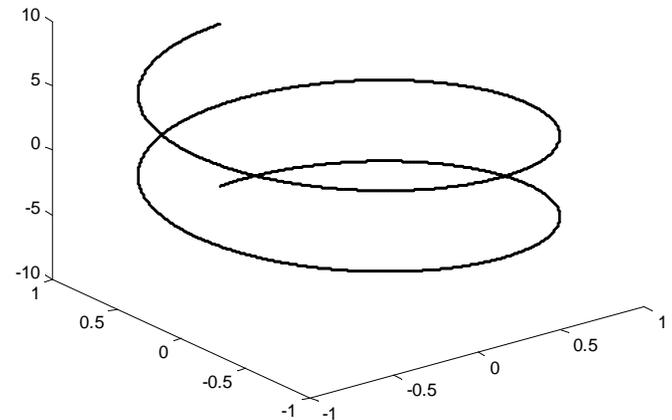
# 3D Line Plots

---

- We can plot in 3 dimensions just as easily as in 2

```
» time=0:0.001:4*pi;  
» x=sin(time);  
» y=cos(time);  
» z=time;  
» plot3(x,y,z,'k','LineWidth',2);  
» zlabel('Time');
```

- Use tools on figure to rotate it
- Can set limits on all 3 axes
  - » `xlim`, `ylim`, `zlim`



# Surface Plots

---

- It is more common to visualize *surfaces* in 3D

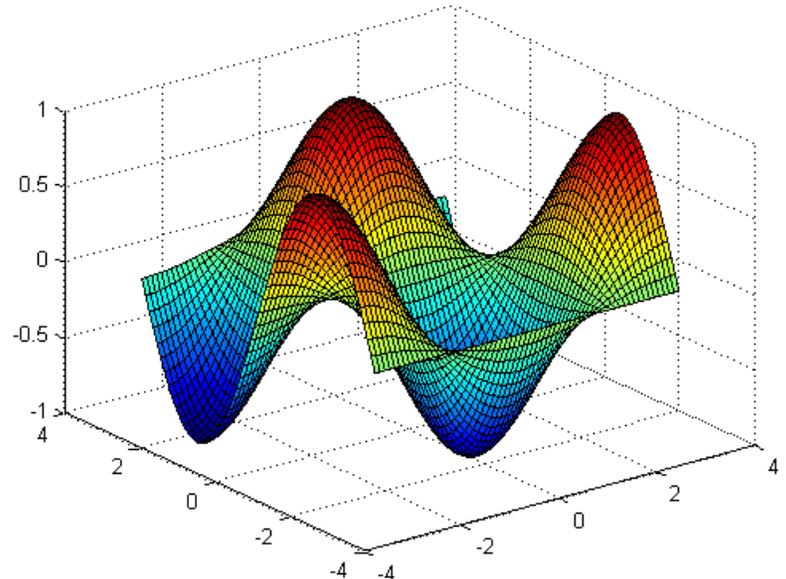
- Example:

$$\begin{array}{l} f(x, y) = \sin(x)\cos(y) \\ x \in [-\pi, \pi]; y \in [-\pi, \pi] \end{array}$$

- **surf** puts vertices at specified points in space  $x, y, z$ , and connects all the vertices to make a surface
- The vertices can be denoted by matrices  $X, Y, Z$
- How can we make these matrices
  - loop (DUMB)
  - built-in function: **meshgrid**

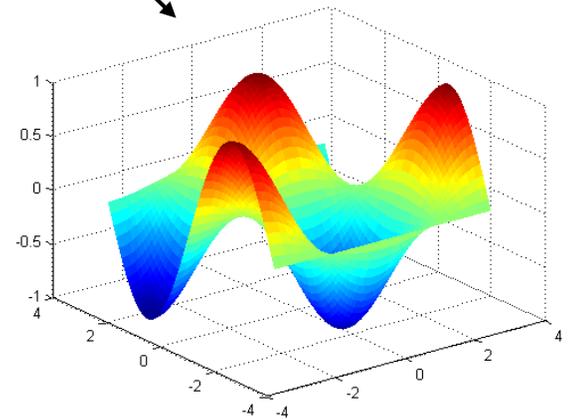
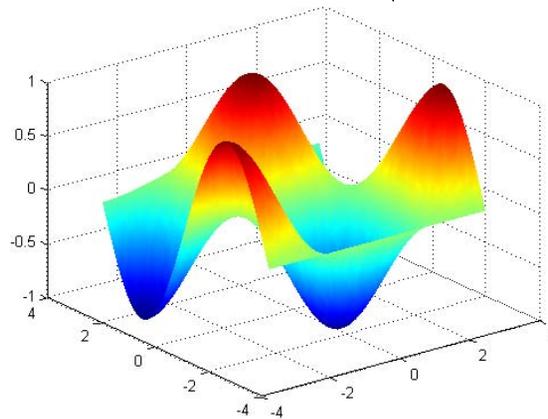
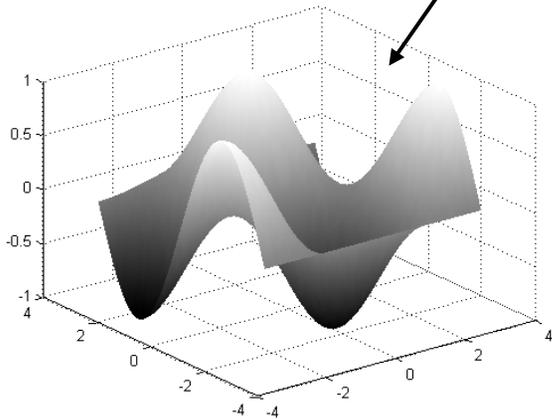
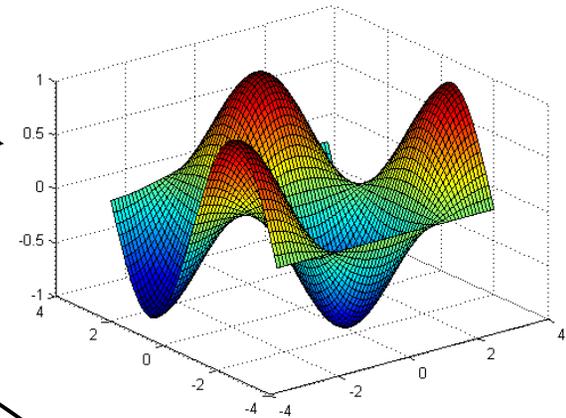
# surf

- Make the x and y vectors
  - » `x=-pi:0.1:pi;`
  - » `y=-pi:0.1:pi;`
- Use meshgrid to make matrices (this is the same as loop)
  - » `[X,Y]=meshgrid(x,y);`
- To get function values, evaluate the matrices
  - » `Z =sin(X).*cos(Y);`
- Plot the surface
  - » `surf(X,Y,Z)`
  - » `surf(x,y,Z);`



# surf Options

- See **help surf** for more options
- There are three types of surface shading
  - » **shading faceted**
  - » **shading flat**
  - » **shading interp**
- You can change colormaps
  - » **colormap(gray)**



# contour

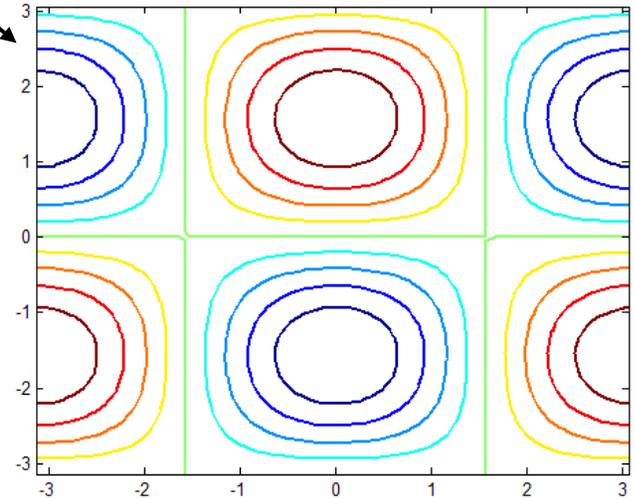
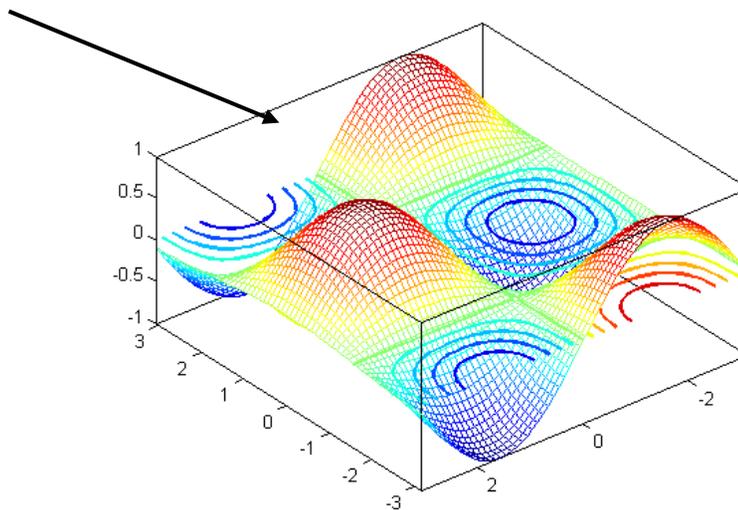
- You can make surfaces two-dimensional by using contour

» `contour(X,Y,Z,'LineWidth',2)`

- takes same arguments as surf
- color indicates height
- can modify linestyle properties
- can set colormap

» `hold on`

» `mesh(X,Y,Z)`

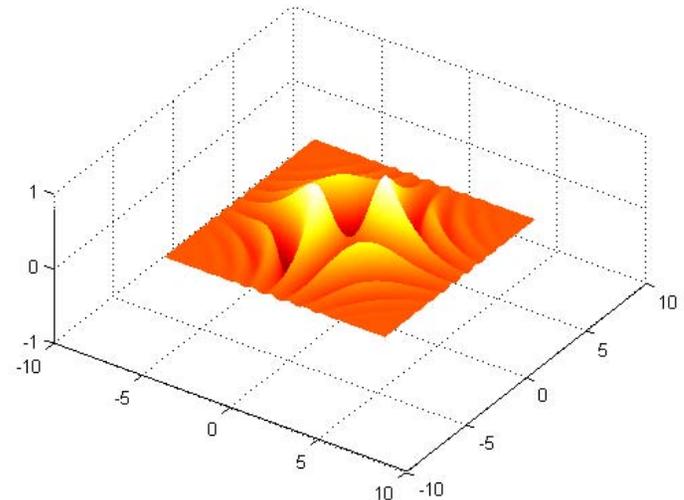


# Exercise: 3-D Plots

---

- Plot  $\exp(-.1(x^2+y^2))\sin(xy)$  for  $x,y$  in  $[-2\pi, 2\pi]$  with interpolated shading and a hot colormap:

```
» x=-2*pi:0.1:2*pi;  
» y=-2*pi:0.1:2*pi;  
» [X,Y]=meshgrid(x,y);  
» Z =exp(-.1*(X.^2+Y.^2)).*sin(X.*Y);  
» surf(X,Y,Z);  
» shading interp  
» colormap hot
```



# Specialized Plotting Functions

---

- MATLAB has a lot of specialized plotting functions
- **polar**-to make polar plots
  - » `polar(0:0.01:2*pi,cos((0:0.01:2*pi)*2))`
- **bar**-to make bar graphs
  - » `bar(1:10,rand(1,10));`
- **quiver**-to add velocity vectors to a plot
  - » `[X,Y]=meshgrid(1:10,1:10);`
  - » `quiver(X,Y,rand(10),rand(10));`
- **stairs**-plot piecewise constant functions
  - » `stairs(1:10,rand(1,10));`
- **fill**-draws and fills a polygon with specified vertices
  - » `fill([0 1 0.5],[0 0 1],'r');`
- see help on these functions for syntax
- **doc specgraph** – for a complete list

# Outline

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(1) Plotting Continued

**(2) Scripts**

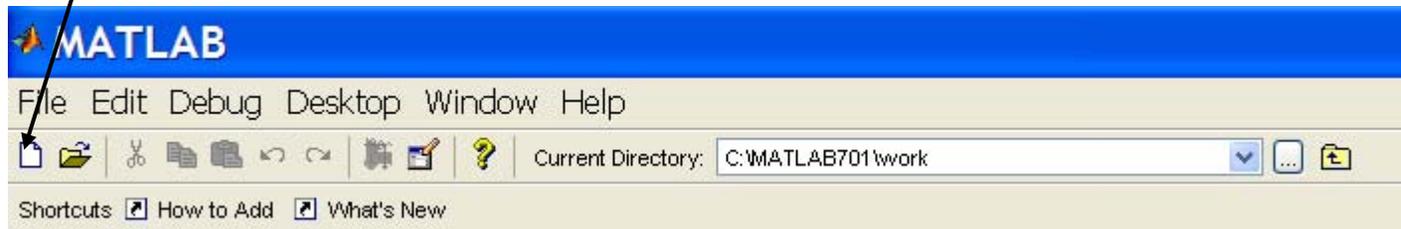
(3) Functions

(4) Flow Control

# Scripts: Overview

---

- Scripts are
  - written in the MATLAB editor
  - saved as MATLAB files (.m extension)
  - evaluated line by line
- To create an MATLAB file from command-line
  - » `edit myScript.m`
- or click



Courtesy of The MathWorks, Inc. Used with permission.

# Scripts: the Editor

\* Means that it's not saved

Line numbers

MATLAB file path

Debugging tools

```
1 % coinToss.m
2 % a script that flips a fair coin and displays the output
3
4 if rand < 0.5 % if random number is less than 0.5 say heads
5     disp('HEADS');
6 else % if greater than 0.5, say tails
7     disp('TAILS');
8 end
```

Possible breakpoints

Courtesy of The MathWorks, Inc. Used with permission.

# Scripts: Good Practice

---

- Take advantage of "smart indent" option
- Keep code clean
  - Use built-in functions
  - Vectorize, vectorize, vectorize
  - When making large matrices, allocate space first
    - Use nan or zeros to make a matrix of the desired size
- Keep constants at the top of the MATLAB file
- **COMMENT!**
  - Anything following a % is seen as a comment
  - The first contiguous comment becomes the script's help file
  - Comment thoroughly to avoid wasting time later

# Hello World

---

- Here are several flavors of Hello World to introduce MATLAB
- MATLAB will display strings automatically
  - » `'Hello 6.094'`
- To remove "ans =", use `disp()`
  - » `disp('Hello 6.094')`
- `sprintf()` allows you to mix strings with variables
  - » `class=6.094;`
  - » `disp(sprintf('Hello %g', class))`
    - The format is C-syntax

# Exercise: Scripts

---

- A student has taken three exams. The performance on the exams is random (uniform between 0 and 100)
- The first exam is worth 20%, the second is worth 30%, and the final is worth 50% of the grade
- Calculate the student's overall score
- Save script as practiceScript.m and run a few times

```
» scores=rand(1,3)*100;  
» weights=[0.2 0.3 0.5];  
» overall=scores*weights'
```

# Outline

---

(1) Plotting Continued

(2) Scripts

**(3) Functions**

(4) Flow Control

# User-defined Functions

- Functions look exactly like scripts, but for **ONE** difference
  - Functions must have a function declaration

```
1 % stats: computes the average, standard deviation, and range
2 % of a given vector of data
3 %
4 % [avg,sd,range]=stats(x)
5 % avg - the average (arithmetic mean) of x
6 % sd - the standard deviation of x
7 % range - a 2x1 vector containing the min and max values in x
8 % x - a vector of values
9 function [avg,sd,range]=stats(x)
10 avg=mean(x);
11 sd=std(x);
12 range=[min(x); max(x)];
```

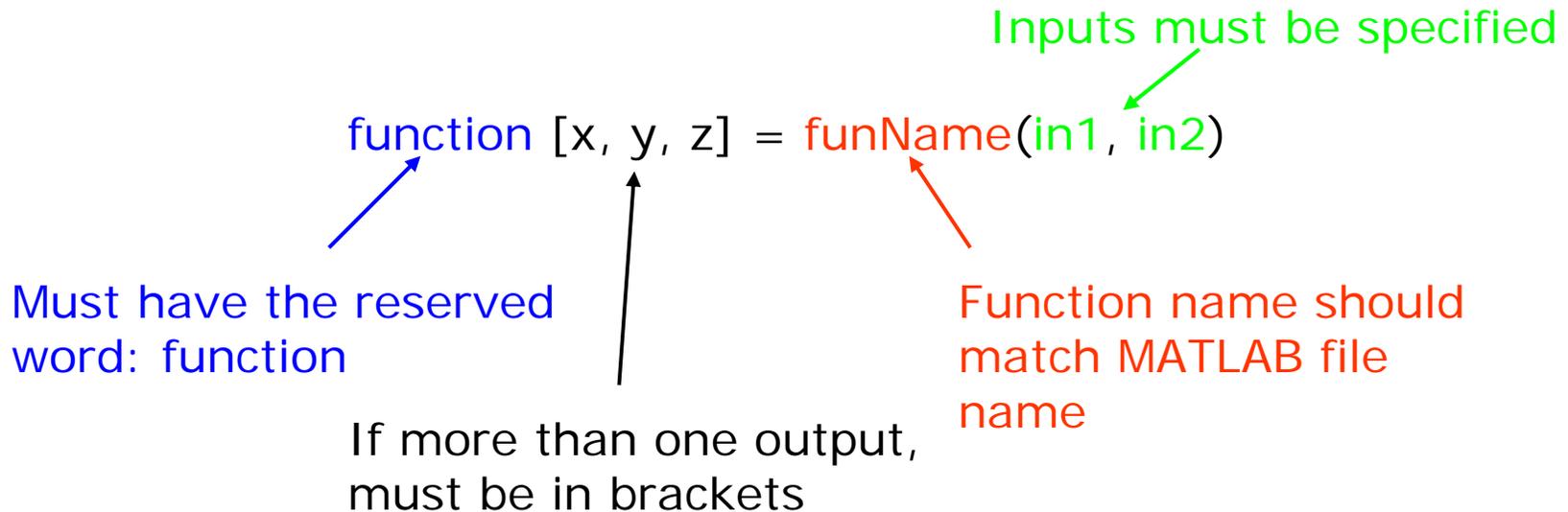
Annotations in the image:

- Help file**: Three arrows point to the first three lines of comments.
- Function declaration**: An arrow points to line 9, `function [avg,sd,range]=stats(x)`.
- Inputs**: An arrow points to `x` in the function declaration.
- Outputs**: An arrow points to the output list `[avg,sd,range]` in the function declaration.

# User-defined Functions

---

- Some comments about the function declaration



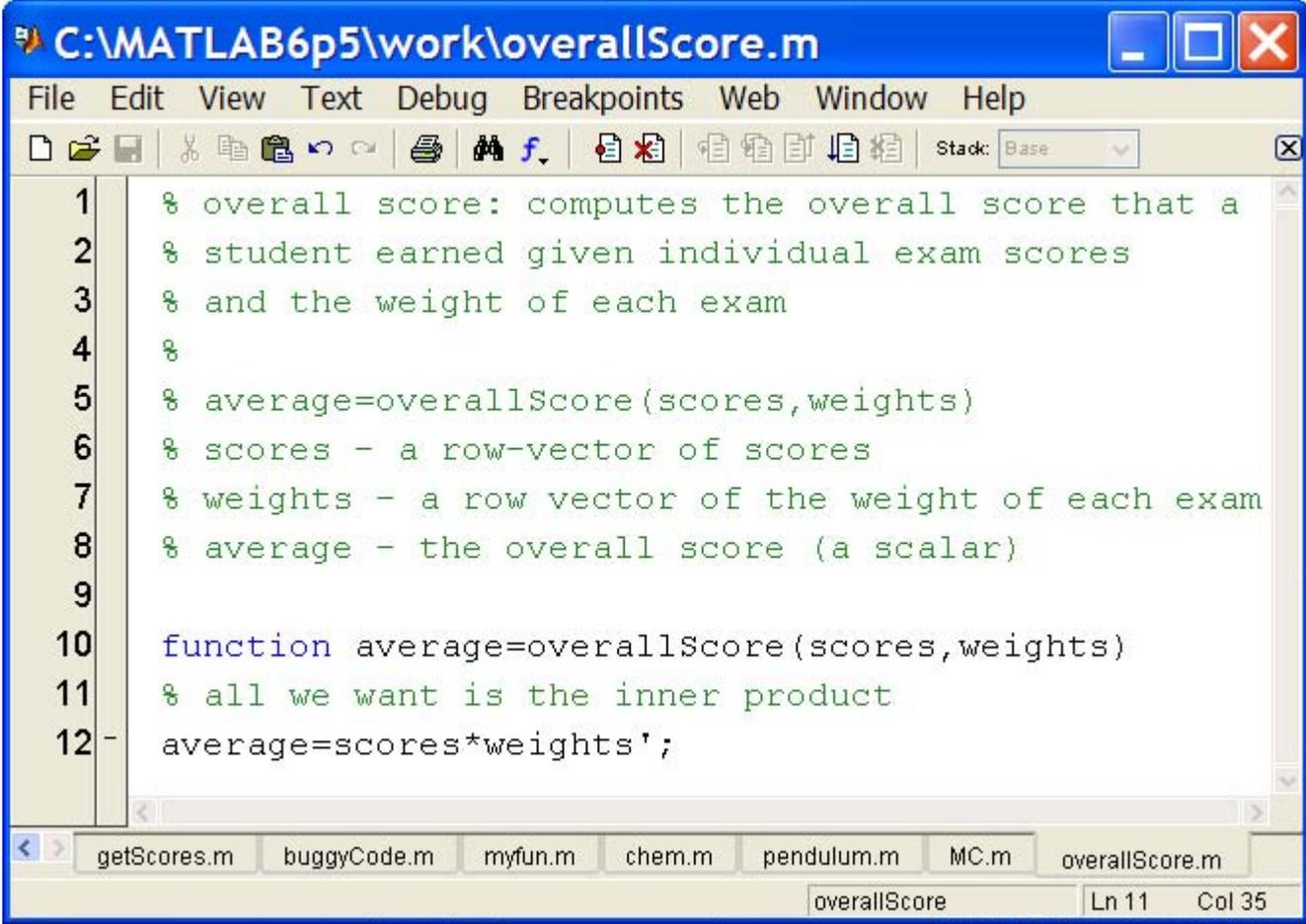
- **No need for return:** MATLAB returns the variables whose names match those in the function declaration
- **Variable scope:** Any variables created within the function but not returned disappear after the function stops running
- Can have variable input arguments (see **help varargin**)

# Functions: Exercise

---

- Take the script we wrote to calculate the student's overall score and make it into a function
- The inputs should be
  - the scores row vector
  - the weight row vector, with the same length as scores
- The output should be
  - A scalar: the overall score
- Assume the user knows the input constraints (no need to check if the inputs are in the correct format\size)
- Name the function overallScore.m

# Functions: Exercise



The image shows a screenshot of a MATLAB editor window titled "C:\MATLAB6p5\work\overallScore.m". The window contains the following code:

```
1 % overall score: computes the overall score that a
2 % student earned given individual exam scores
3 % and the weight of each exam
4 %
5 % average=overallScore(scores,weights)
6 % scores - a row-vector of scores
7 % weights - a row vector of the weight of each exam
8 % average - the overall score (a scalar)
9
10 function average=overallScore(scores,weights)
11 % all we want is the inner product
12 average=scores*weights';
```

The window also shows a toolbar with various icons, a menu bar with "File", "Edit", "View", "Text", "Debug", "Breakpoints", "Web", "Window", and "Help", and a taskbar at the bottom with several open files: "getScores.m", "buggyCode.m", "myfun.m", "chem.m", "pendulum.m", "MC.m", and "overallScore.m". The status bar at the bottom right indicates "overallScore" and "Ln 11 Col 35".

Courtesy of The MathWorks, Inc. Used with permission.

# Functions

---

- We're familiar with
  - » `zeros`
  - » `size`
  - » `length`
  - » `sum`
- Look at the help file for size by typing
  - » `help size`
- The help file describes several ways to invoke the function
  - `D = SIZE(X)`
  - `[M,N] = SIZE(X)`
  - `[M1,M2,M3,...,MN] = SIZE(X)`
  - `M = SIZE(X,DIM)`

# Functions

---

- MATLAB functions are generally overloaded
  - Can take a variable number of inputs
  - Can return a variable number of outputs
- What would the following commands return:
  - » `a=zeros(2,4,8);`
  - » `D=size(a)`
  - » `[m,n]=size(a)`
  - » `[x,y,z]=size(a)`
  - » `m2=size(a,2)`
- Take advantage of overloaded methods to make your code cleaner!

# Outline

---

(1) Plotting Continued

(2) Scripts

(3) Functions

**(4) Flow Control**

# Relational Operators

---

- MATLAB uses *mostly* standard relational operators
  - equal ==
  - **not** equal ~=
  - greater than >
  - less than <
  - greater or equal >=
  - less or equal <=
- Logical operators

	normal	bitwise
➤ And	&	&&
➤ Or		
➤ <b>Not</b>	~	
➤ Xor	xor	
➤ All true	all	
➤ Any true	any	
- Boolean values: zero is false, nonzero is true
- See **help .** for a detailed list of operators

# if/else/elseif

---

- Basic flow-control, common to all languages
- MATLAB syntax is somewhat unique

**IF**

```
if cond
    commands
end
```

Conditional statement:  
evaluates to true or false

**ELSE**

```
if cond
    commands1
else
    commands2
end
```

**ELSEIF**

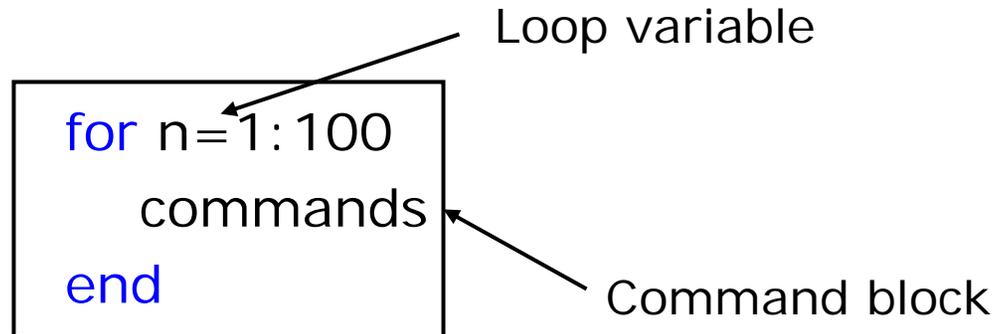
```
if cond1
    commands1
elseif cond2
    commands2
else
    commands3
end
```

- **No need for parentheses:** command blocks are between reserved words

# for

---

- for loops: use for a definite number of iterations
- MATLAB syntax:



- The loop variable
  - Is defined as a vector
  - Is a scalar within the command block
  - Does not have to have consecutive values
- The command block
  - Anything between the **for** line and the **end**

# while

---

- The while is like a more general for loop:
  - Don't need to know number of iterations

```
        WHILE
while cond
  commands
end
```

- The command block will execute while the conditional expression is true
- Beware of infinite loops!

# Exercise: Control-Flow

---

- Write a function to calculate the factorial of an integer N using a loop (you can use a for or while loop). If the input is less than 0, return NaN. Test it using some values.

```
» function a = factorial(N)
» if N<0,
»     a=nan,
» else
»     a = 1;
»     for k=1:N
»         a = a*k;
»     end
» end
```

- But note that factorial() is already implemented! You should see if there are built-in functions before implementing something yourself.
  - » `which factorial`

# find

---

- **find** is a very important function
  - Returns indices of nonzero values
  - Can simplify code and help avoid loops
- Basic syntax: `index=find(cond)`
  - » `x=rand(1,100);`
  - » `inds = find(x>0.4 & x<0.6);`
- `inds` will contain the indices at which `x` has values between 0.4 and 0.6. This is what happens:
  - `x>0.4` returns a vector with 1 where true and 0 where false
  - `x<0.6` returns a similar vector
  - The `&` combines the two vectors using an and
  - The `find` returns the indices of the 1's

# Exercise: Flow Control

---

- Given  $x = \sin(\text{linspace}(0, 10 * \pi, 100))$ , how many of the entries are positive?

Using a loop and if/else

```
count=0;
for n=1:length(x)
    if x(n)>0
        count=count+1;
    end
end
```

Being more clever

```
count=length(find(x>0));
```

length(x)	Loop time	Find time
100	0.01	0
10,000	0.1	0
100,000	0.22	0
1,000,000	1.5	0.04

- Avoid loops like the plague!
- Built-in functions will make it faster to write and execute

# Efficient Code

---

- Avoid loops whenever possible
  - This is referred to as vectorization
- Vectorized code is more efficient for MATLAB
- Use indexing and matrix operations to avoid loops
- For example:
  - » `a=rand(1,100);`
  - » `b=zeros(1,100);`
  - » `for n=1:100`
    - » `if n==1`
      - » `b(n)=a(n);`
      - » `else`
        - » `b(n)=a(n-1)+a(n);`
      - » `end`
    - » `end`
      - Slow and complicated
  - » `a=rand(1,100);`
  - » `b=[0 a(1:end-1)]+a;`
    - Efficient and clean

# Exercise: Vectorization

---

- Alter your factorial program to work WITHOUT a loop. Use **prod**
  - » `function a=factorial(N)`
  - » `a=prod(1:N);`
- You can tic/toc to see how much faster this is than the loop!
- **BUT**...Don't ALWAYS avoid loops
  - Over-vectorizing code can obfuscate it, i.e. you won't be able to understand or debug it later
  - Sometime a loop is the right thing to do, it is clearer and simple

# End of Lecture 2

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- (1) Plotting Continued
- (2) Scripts
- (3) Functions
- (4) Flow Control

**Vectorization makes  
coding fun!**

