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6.094 Introduction to MATLAB®
January (IAP) 2009

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6.094

Introduction to Programming in MATLAB®

Lecture 2: Visualization and Programming

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IAP 2009

Outline

(1) Plotting Continued

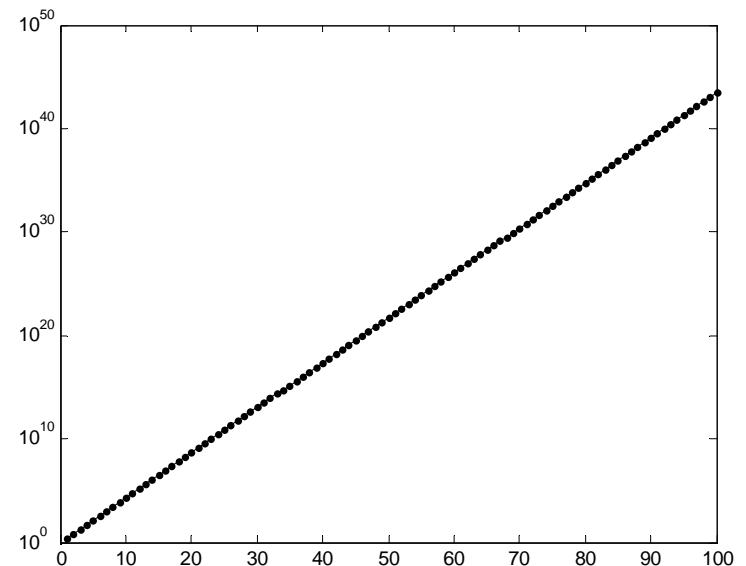
(2) Scripts

(3) Functions

(4) Flow Control

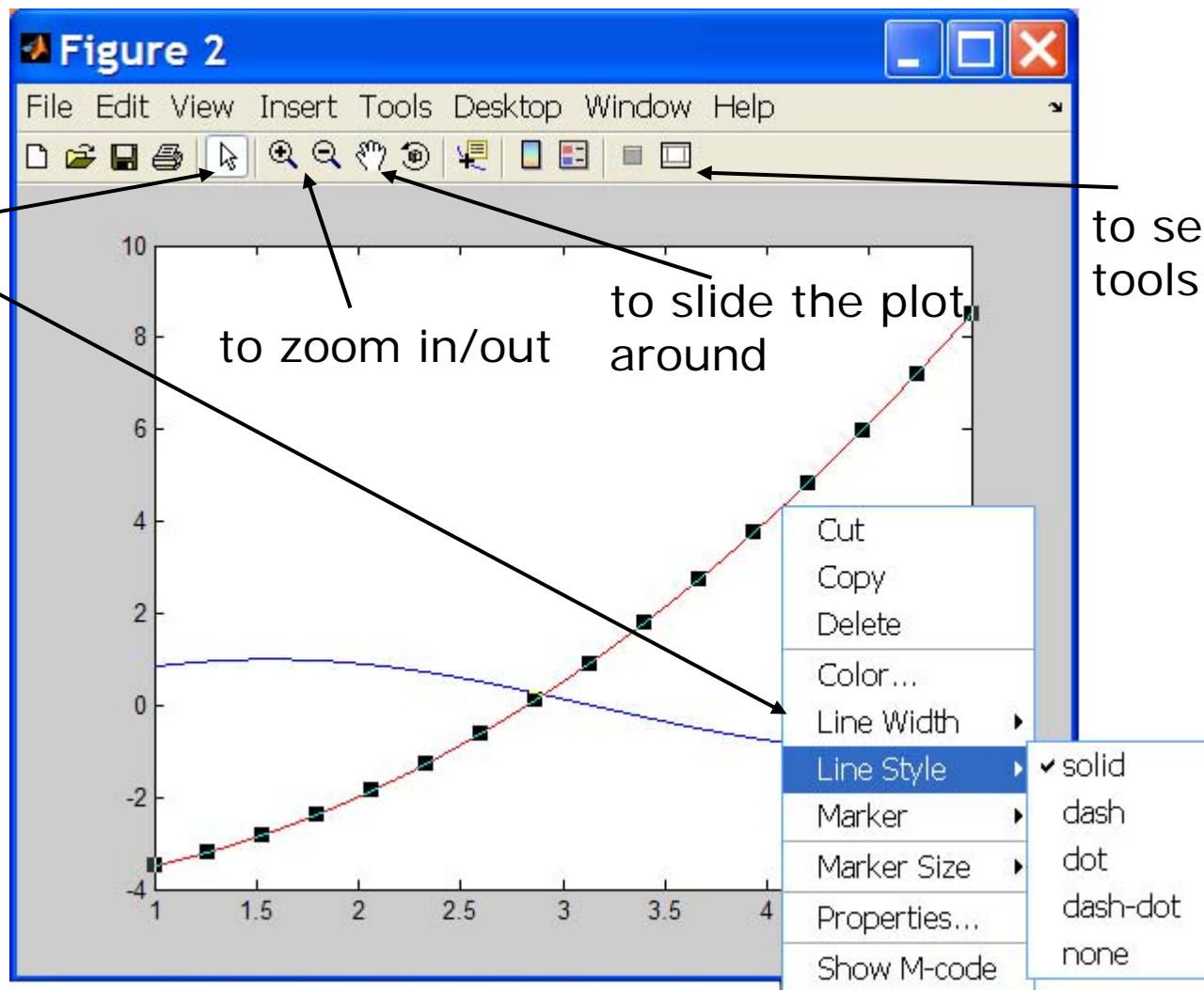
Cartesian Plots

- We have already seen the plot function
 - » `x=-pi:pi/100:pi;`
 - » `y=cos(4*x).*sin(10*x).*exp(-abs(x));`
 - » `plot(x,y,'k-');`
- The same syntax applies for semilog and loglog plots
 - » `semilogx(x,y,'k');`
 - » `semilogy(y,'r.-');`
 - » `loglog(x,y);`
- For example:
 - » `x=0:100;`
 - » `semilogy(x,exp(x),'k.-');`



Playing with the Plot

to select lines
and delete or
change
properties

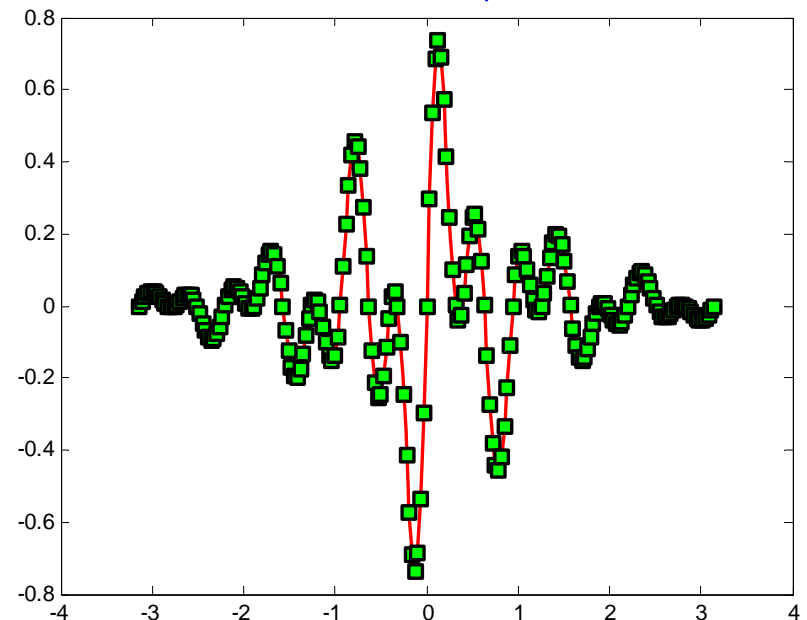


Courtesy of The MathWorks, Inc. Used with permission.

Line and Marker Options

- Everything on a line can be customized
 - » `plot(x,y,'--rs','LineWidth',2,...`
`'MarkerEdgeColor','k',...`
`'MarkerFaceColor','g',...`
`'MarkerSize',10)`

- See **doc line** for a full list of properties that can be specified



Labels

- Last time we saw how to add titles and labels using the GUI. Can also do it command-line:

- » `title('Stress-Strain');`

- » `xlabel('Force (N)');`

- For multiple lines, add a legend entry for each line

- » `legend('Steel','Aluminum','Tungsten');`

- Can specify font and size for the text

- » `ylabel('Distance (m)','FontSize',14,...`

- `'FontName','Helvetica');`

- use ... to break long commands across multiple lines

- To put parameter values into labels, need to use **num2str** and concatenate:

- » `str = ['Strength of ' num2str(d) 'cm diameter rod'];`

- » `title(str)`

Axis

- A grid makes it easier to read values
 - » `grid on`
- `xlim` sets only the x axis limits
 - » `xlim([-pi pi]);`
- `ylim` sets only the y axis limits
 - » `ylim([-1 1]);`
- To specify both at once, use `axis`:
 - » `axis([-pi pi -1 1]);`
 - sets the x axis limits between -pi and pi and the y axis limits between -1 and 1
- Can specify tickmarks
 - » `set(gca, 'XTick', linspace(-pi, pi, 3))`
 - see `doc axes` for a list of properties you can set this way
 - more on advanced figure customization in lecture 4

Axis Modes

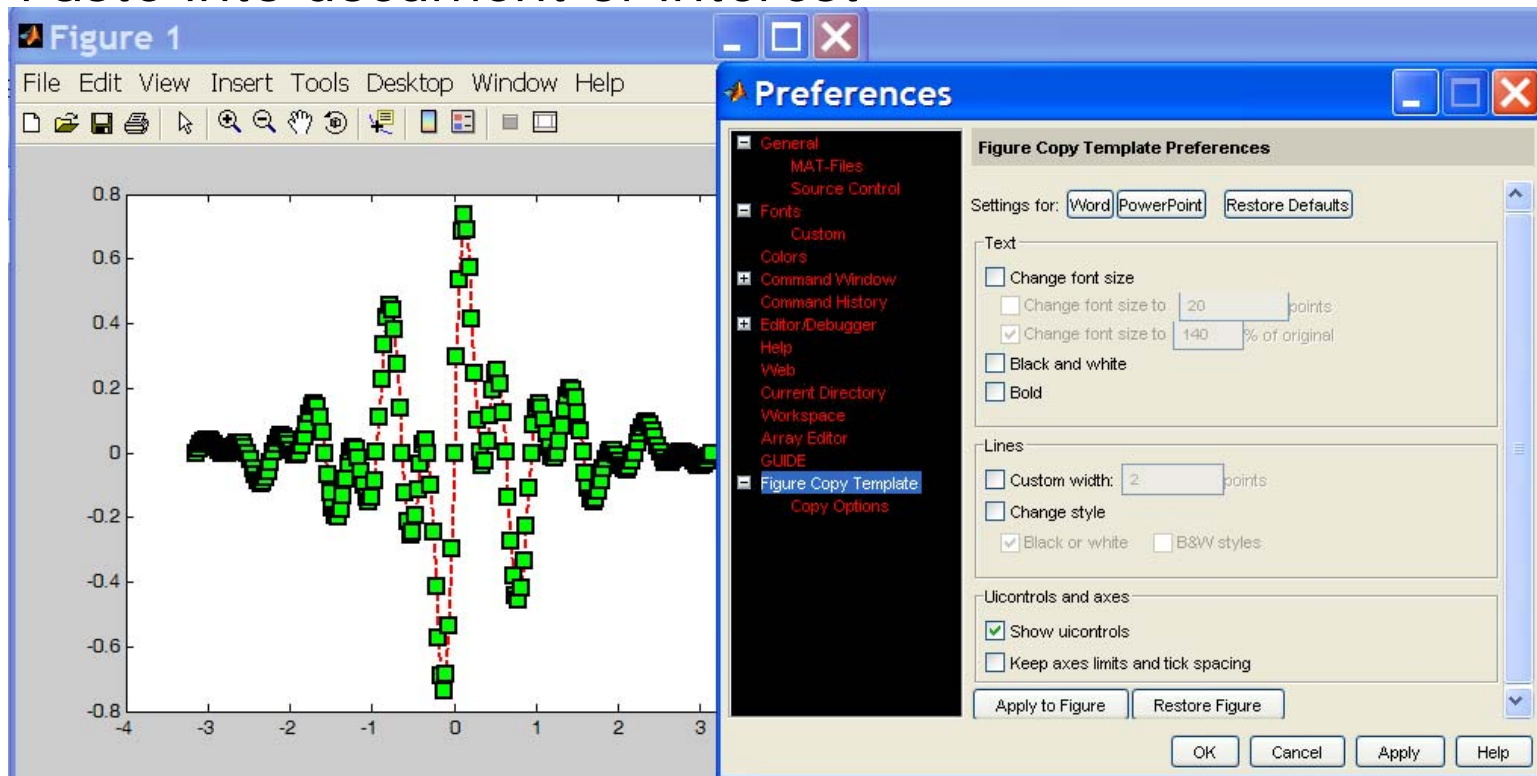
- Built-in axis modes
 - » **axis square**
 - makes the current axis look like a box
 - » **axis tight**
 - fits axes to data
 - » **axis equal**
 - makes x and y scales the same
 - » **axis xy**
 - puts the origin in the bottom left corner (default)
 - » **axis ij**
 - puts the origin in the top left corner (for viewing matrices)

Multiple Plots in one Figure

- Use the figure command to open a new figure
 - » `figure`
- or activate an open figure
 - » `figure(1)`
- To have multiple axes in one figure
 - » `subplot(2,3,1)` or `subplot(231)`
 - makes a figure with 2 rows and three columns of axes, and activates the first axis for plotting
 - each axis can have labels, a legend, and a title
 - » `subplot(2,3,4:6)`
 - activating a range of axes fuses them into one
- To close existing figures
 - » `close([1 3])`
 - closes figures 1 and 3
 - » `close all`
 - closes all figures (useful in scripts/functions)

Copy/Paste Figures

- Figures can be pasted into other apps (word, ppt, etc)
- *Edit* → *copy options* → *figure copy template*
 - Change font sizes, line properties; presets for word and ppt
- *Edit* → *copy figure* to copy figure
- Paste into document of interest



Saving Figures

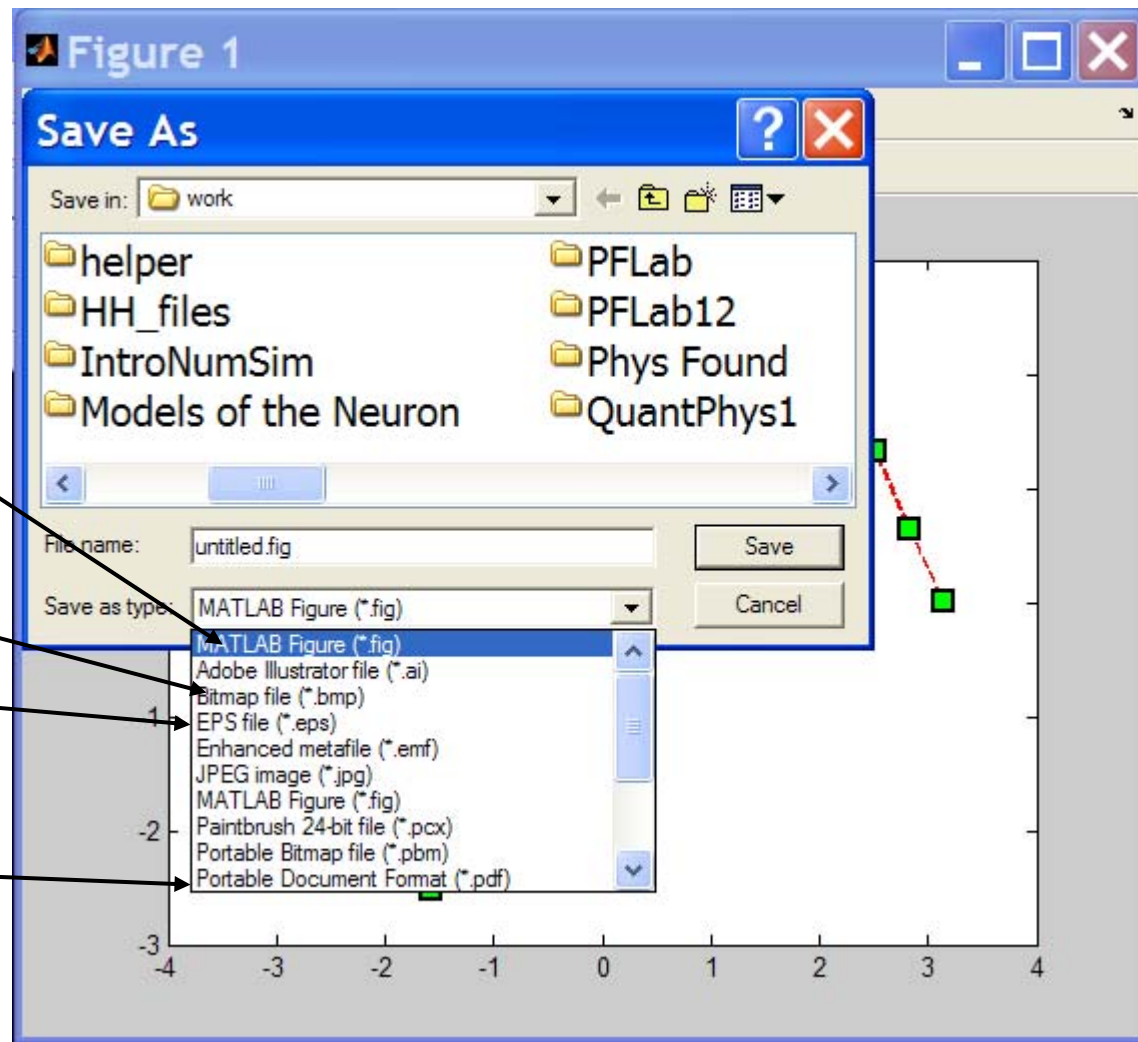
- Figures can be saved in many formats. The common ones are:

.fig preserves all information

.bmp uncompressed image

.eps high-quality scaleable format

.pdf compressed image



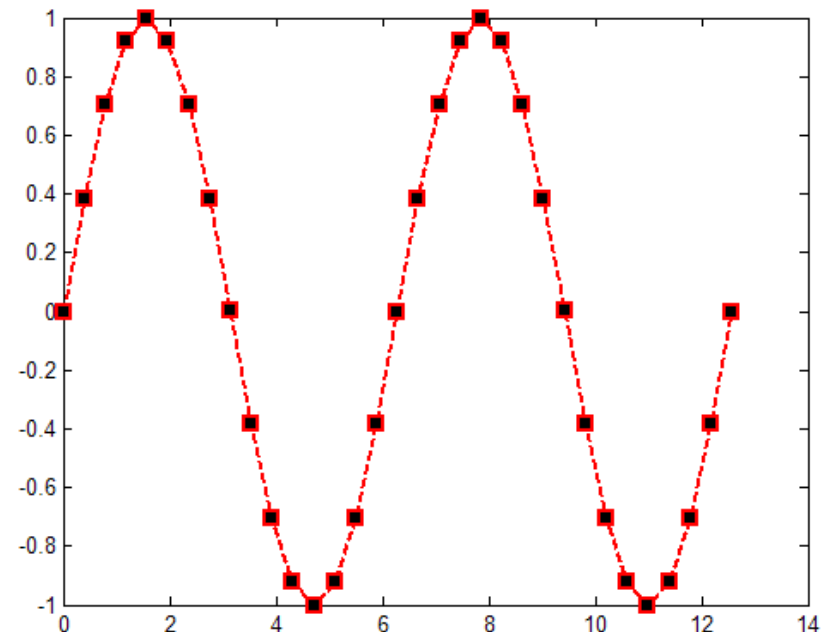
Figures: Exercise

- Open a figure and plot a sine wave over two periods with data points at $0, \pi/8, 2\pi/8, \dots$. Use black squares as markers and a dashed red line of thickness 2 as the line

» `figure`

» `plot(0:pi/4:4*pi,sin(0:pi/4:4*pi),'rs--',...
 'LineWidth',2,'MarkerFaceColor','k');`

- Save the figure as a pdf
- View with pdf viewer.



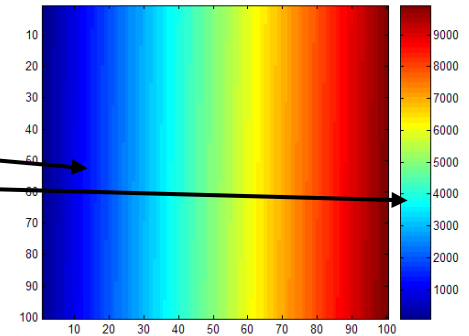
Visualizing matrices

- Any matrix can be visualized as an image

- » `mat=reshape(1:10000,100,100);`

- » `imagesc(mat);`

- » `colorbar`



- **imagesc** automatically scales the values to span the entire colormap
- Can set limits for the color axis (analogous to `xlim`, `ylim`)
 - » `caxis([3000 7000])`

Colormaps

- You can change the colormap:

- » `imagesc(mat)`

- default map is `jet`

- » `colormap(gray)`

- » `colormap(cool)`

- » `colormap(hot(256))`

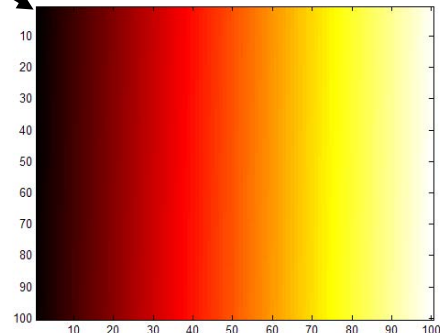
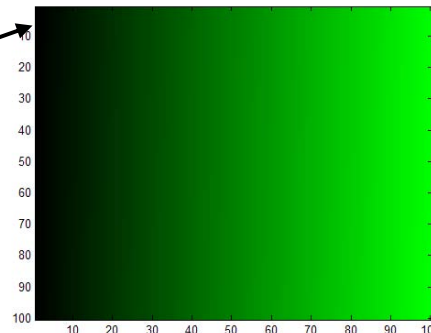
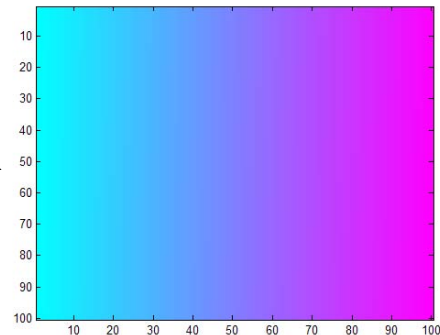
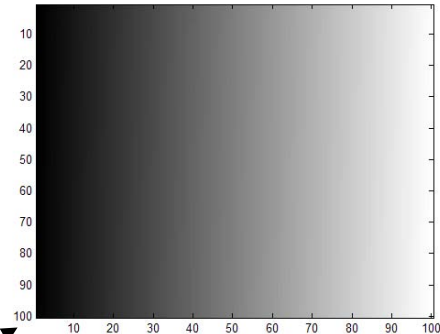
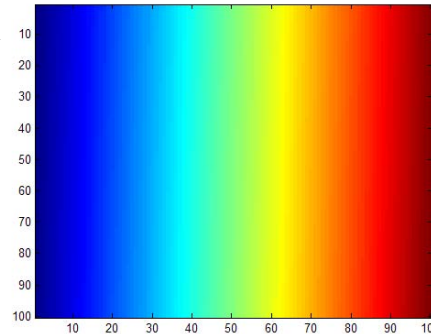
- See `help hot` for a list

- Can define custom colormap

- » `map=zeros(256,3);`

- » `map(:,2)=(0:255)/255;`

- » `colormap(map);`



Images: Exercise

- Construct a Discrete Fourier Transform Matrix of size 128 using **dftmtx**
- Display the phase of this matrix as an image using a hot colormap with 256 colors

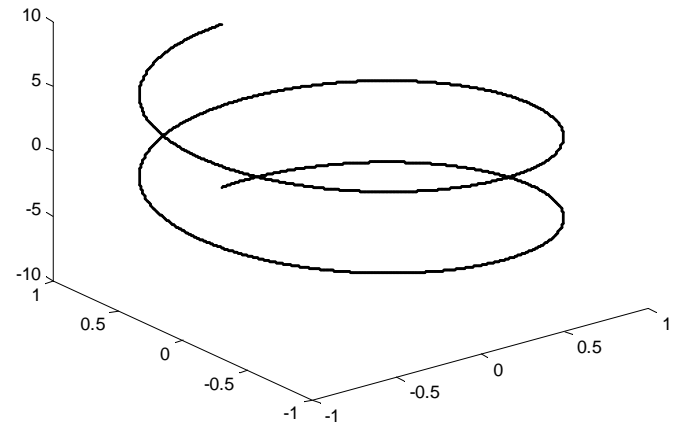
```
» dMat=dftmtx(128);  
» phase=angle(dMat);  
» imagesc(phase);  
» colormap(hot(256));
```

3D Line Plots

- We can plot in 3 dimensions just as easily as in 2

```
» time=0:0.001:4*pi;  
» x=sin(time);  
» y=cos(time);  
» z=time;  
» plot3(x,y,z,'k','LineWidth',2);  
» zlabel('Time');
```

- Use tools on figure to rotate it
- Can set limits on all 3 axes
» `xlim`, `ylim`, `zlim`



Surface Plots

- It is more common to visualize *surfaces* in 3D

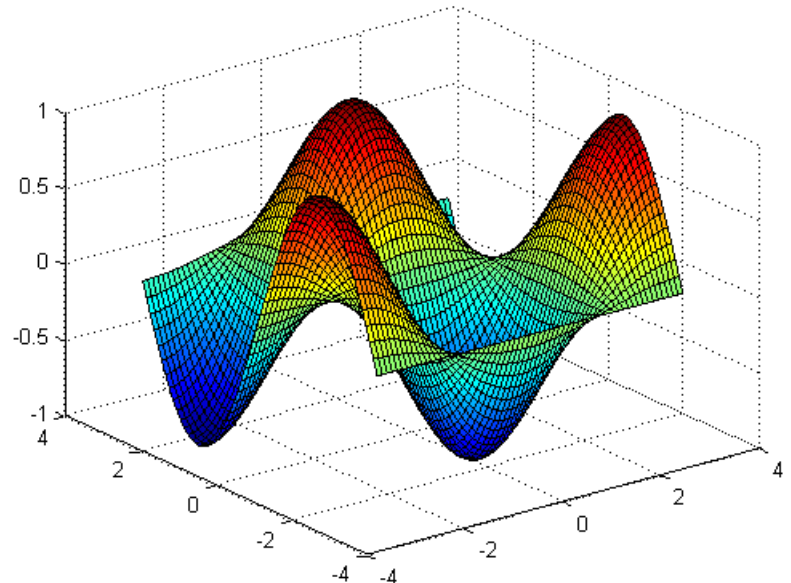
- Example:

$$\begin{aligned} f(x, y) &= \sin(x)\cos(y) \\ x &\in [-\pi, \pi]; y \in [-\pi, \pi] \end{aligned}$$

- **surf** puts vertices at specified points in space x, y, z , and connects all the vertices to make a surface
- The vertices can be denoted by matrices X, Y, Z
- How can we make these matrices
 - loop (DUMB)
 - built-in function: **meshgrid**

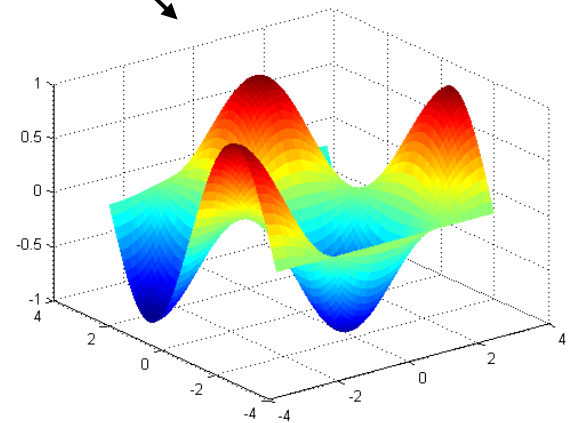
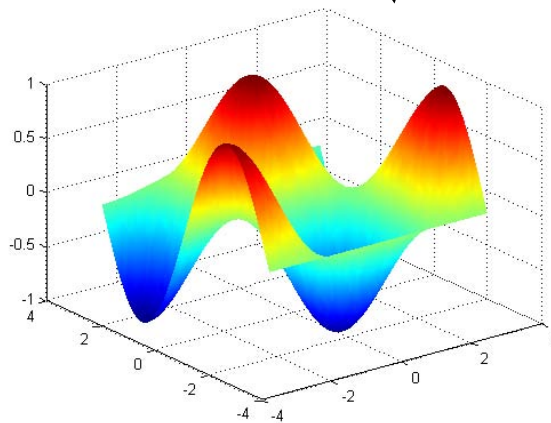
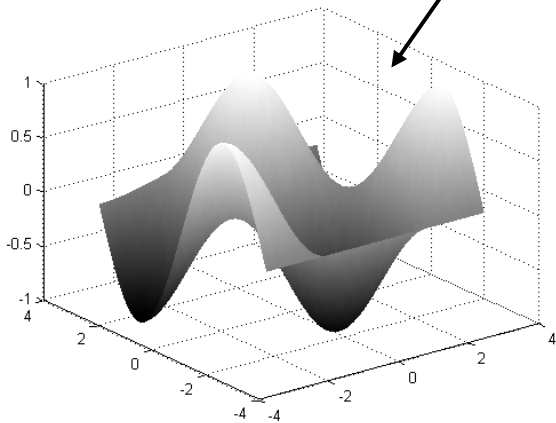
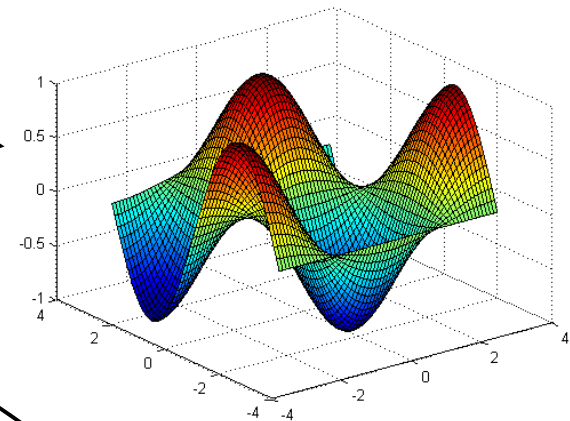
surf

- Make the x and y vectors
 - » `x=-pi:0.1:pi;`
 - » `y=-pi:0.1:pi;`
- Use meshgrid to make matrices (this is the same as loop)
 - » `[X,Y]=meshgrid(x,y);`
- To get function values, evaluate the matrices
 - » `Z =sin(X).*cos(Y);`
- Plot the surface
 - » `surf(X,Y,Z)`
 - » `surf(x,y,Z);`



surf Options

- See **help surf** for more options
- There are three types of surface shading
 - » **shading faceted**
 - » **shading flat**
 - » **shading interp**
- You can change colormaps
 - » **colormap(gray)**



contour

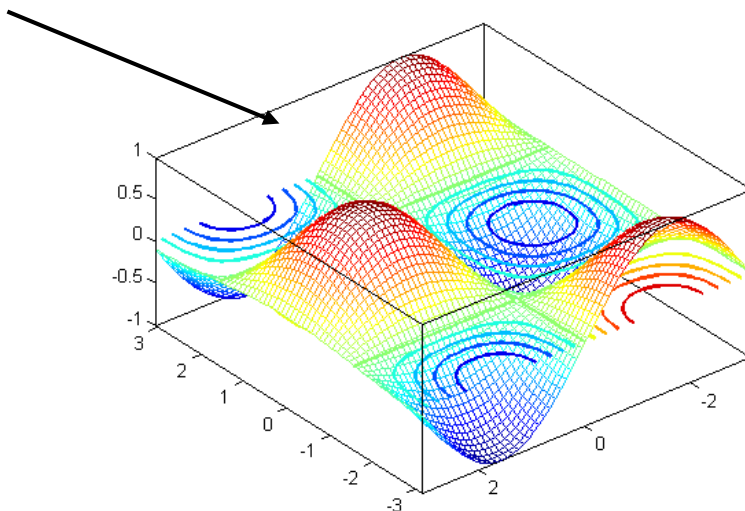
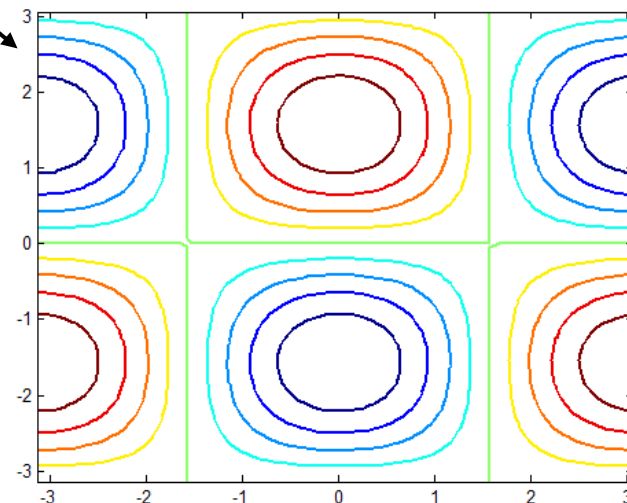
- You can make surfaces two-dimensional by using contour

» `contour(X,Y,Z,'LineWidth',2)`

- takes same arguments as surf
- color indicates height
- can modify linestyle properties
- can set colormap

» `hold on`

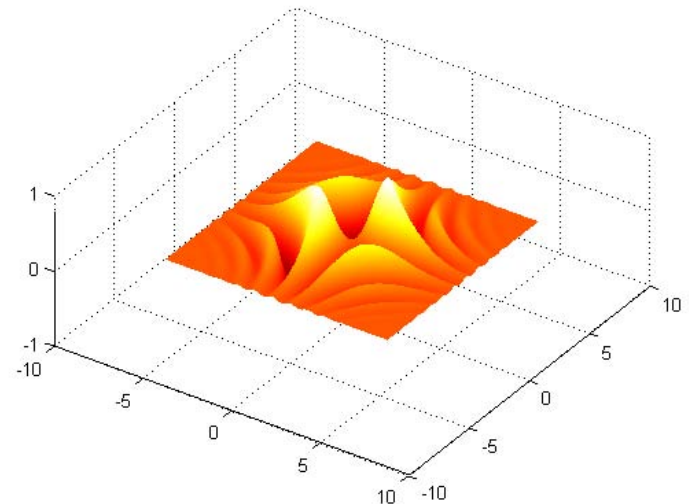
» `mesh(X,Y,Z)`



Exercise: 3-D Plots

- Plot $\exp(-.1(x^2+y^2))\sin(xy)$ for x,y in $[-2\pi, 2\pi]$ with interpolated shading and a hot colormap:

```
» x=-2*pi:0.1:2*pi;  
» y=-2*pi:0.1:2*pi;  
» [X,Y]=meshgrid(x,y);  
» Z =exp(-.1*(X.^2+Y.^2)).*sin(X.*Y);  
» surf(X,Y,Z);  
» shading interp  
» colormap hot
```



Specialized Plotting Functions

- MATLAB has a lot of specialized plotting functions
- **polar**-to make polar plots
 - » `polar(0:0.01:2*pi,cos((0:0.01:2*pi)*2))`
- **bar**-to make bar graphs
 - » `bar(1:10,rand(1,10));`
- **quiver**-to add velocity vectors to a plot
 - » `[X,Y]=meshgrid(1:10,1:10);`
 - » `quiver(X,Y,rand(10),rand(10));`
- **stairs**-plot piecewise constant functions
 - » `stairs(1:10,rand(1,10));`
- **fill**-draws and fills a polygon with specified vertices
 - » `fill([0 1 0.5],[0 0 1],'r');`
- see help on these functions for syntax
- **doc specgraph** – for a complete list

Outline

(1) Plotting Continued

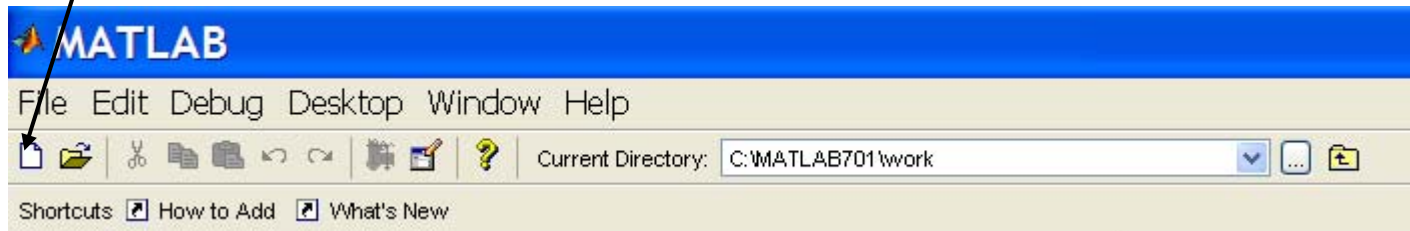
(2) Scripts

(3) Functions

(4) Flow Control

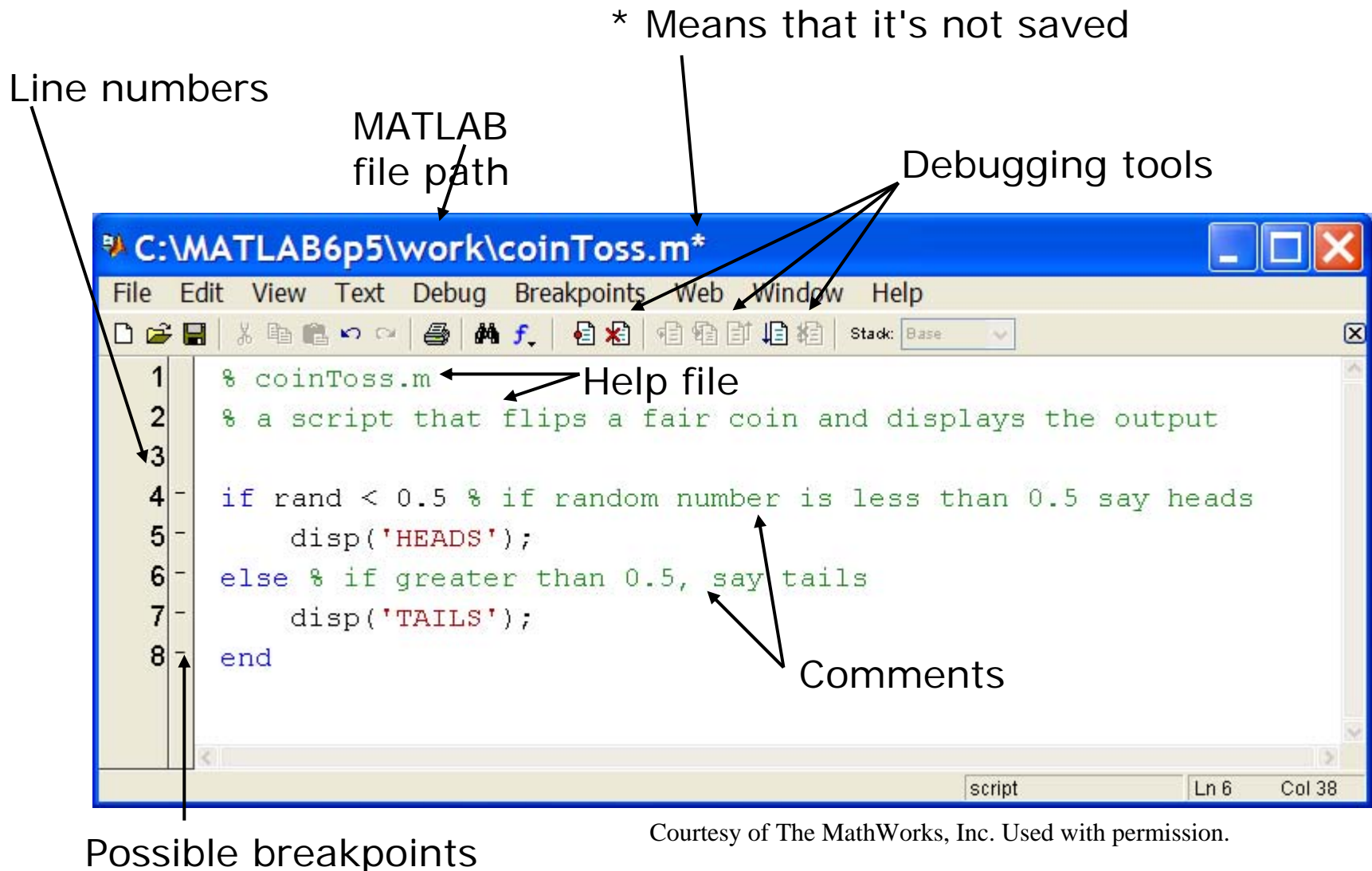
Scripts: Overview

- Scripts are
 - written in the MATLAB editor
 - saved as MATLAB files (.m extension)
 - evaluated line by line
- To create an MATLAB file from command-line
 - » `edit myScript.m`
- or click



Courtesy of The MathWorks, Inc. Used with permission.

Scripts: the Editor



Scripts: Good Practice

- Take advantage of "smart indent" option
- Keep code clean
 - Use built-in functions
 - Vectorize, vectorize, vectorize
 - When making large matrices, allocate space first
 - Use nan or zeros to make a matrix of the desired size
- Keep constants at the top of the MATLAB file
- **COMMENT!**
 - Anything following a % is seen as a comment
 - The first contiguous comment becomes the script's help file
 - Comment thoroughly to avoid wasting time later

Hello World

- Here are several flavors of Hello World to introduce MATLAB
- MATLAB will display strings automatically
 - » `'Hello 6.094'`
- To remove "ans =", use `disp()`
 - » `disp('Hello 6.094')`
- `sprintf()` allows you to mix strings with variables
 - » `class=6.094;`
 - » `disp(sprintf('Hello %g', class))`
 - The format is C-syntax

Exercise: Scripts

- A student has taken three exams. The performance on the exams is random (uniform between 0 and 100)
- The first exam is worth 20%, the second is worth 30%, and the final is worth 50% of the grade
- Calculate the student's overall score
- Save script as practiceScript.m and run a few times

```
» scores=rand(1,3)*100;  
» weights=[0.2 0.3 0.5];  
» overall=scores*weights'
```

Outline

(1) Plotting Continued

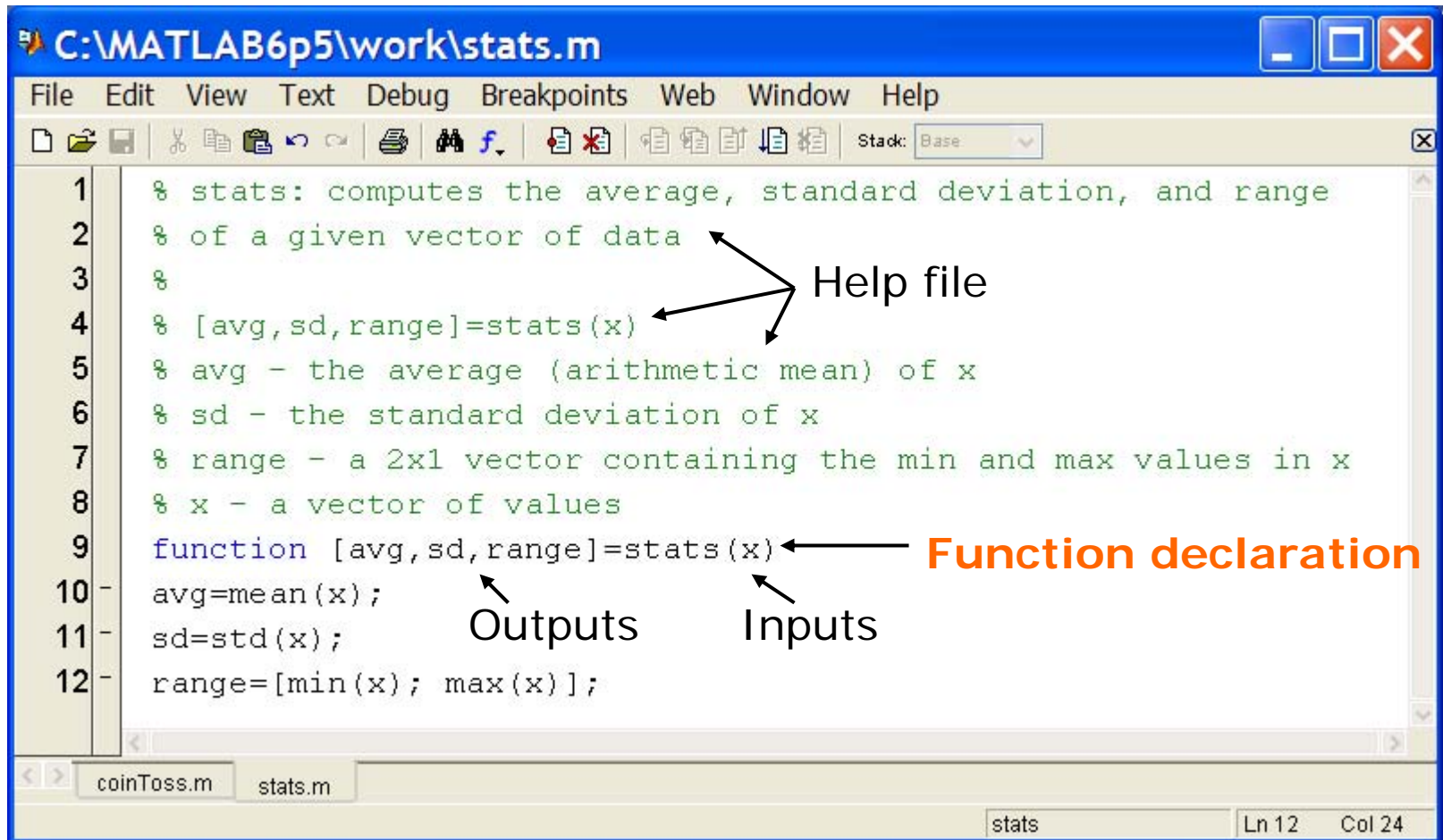
(2) Scripts

(3) Functions

(4) Flow Control

User-defined Functions

- Functions look exactly like scripts, but for **ONE** difference
 - Functions must have a function declaration



The image shows a MATLAB editor window titled 'C:\MATLAB6p5\work\stats.m'. The window contains the following code:

```
1 % stats: computes the average, standard deviation, and range
2 % of a given vector of data
3 %
4 % [avg,sd,range]=stats(x)
5 % avg - the average (arithmetic mean) of x
6 % sd - the standard deviation of x
7 % range - a 2x1 vector containing the min and max values in x
8 % x - a vector of values
9 function [avg,sd,range]=stats(x)
10 avg=mean(x);
11 sd=std(x);
12 range=[min(x); max(x)];
```

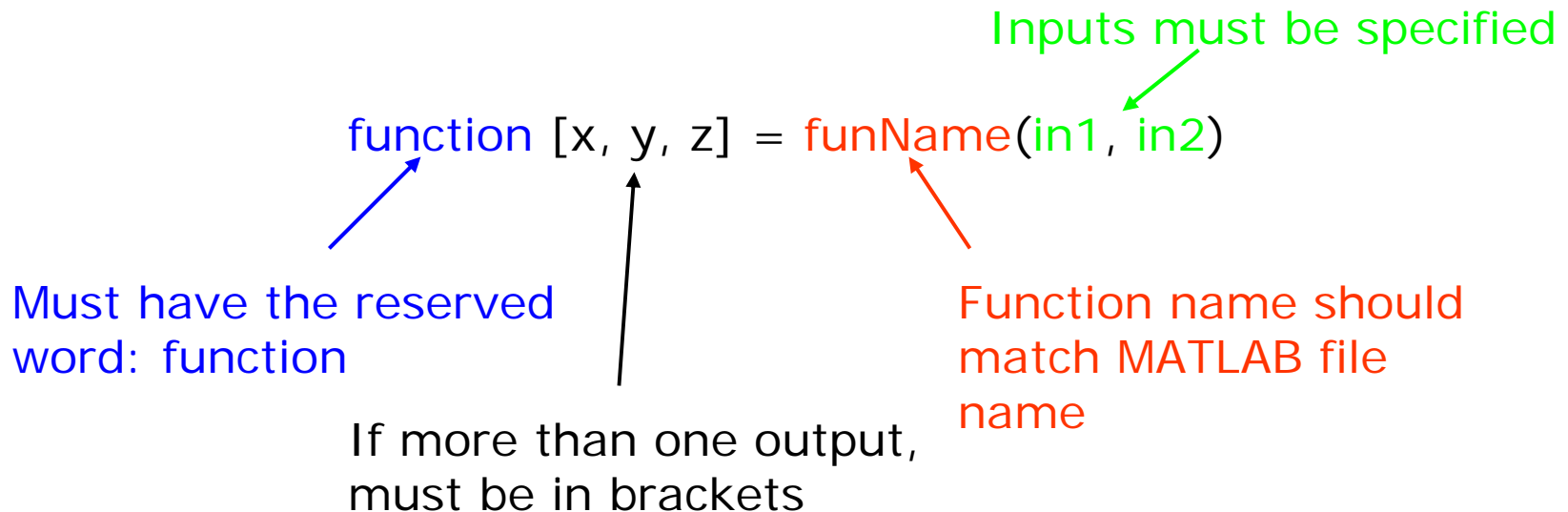
Annotations on the code:

- An arrow points from the text "Help file" to the first three lines of the code (lines 1-3).
- An arrow points from the text "Function declaration" to line 9, which starts with the keyword `function`.
- An arrow points from the text "Outputs" to the output arguments `[avg,sd,range]` in line 9.
- An arrow points from the text "Inputs" to the input argument `x` in line 9.

The window's status bar at the bottom shows 'stats' and 'Ln 12 Col 24'.

User-defined Functions

- Some comments about the function declaration

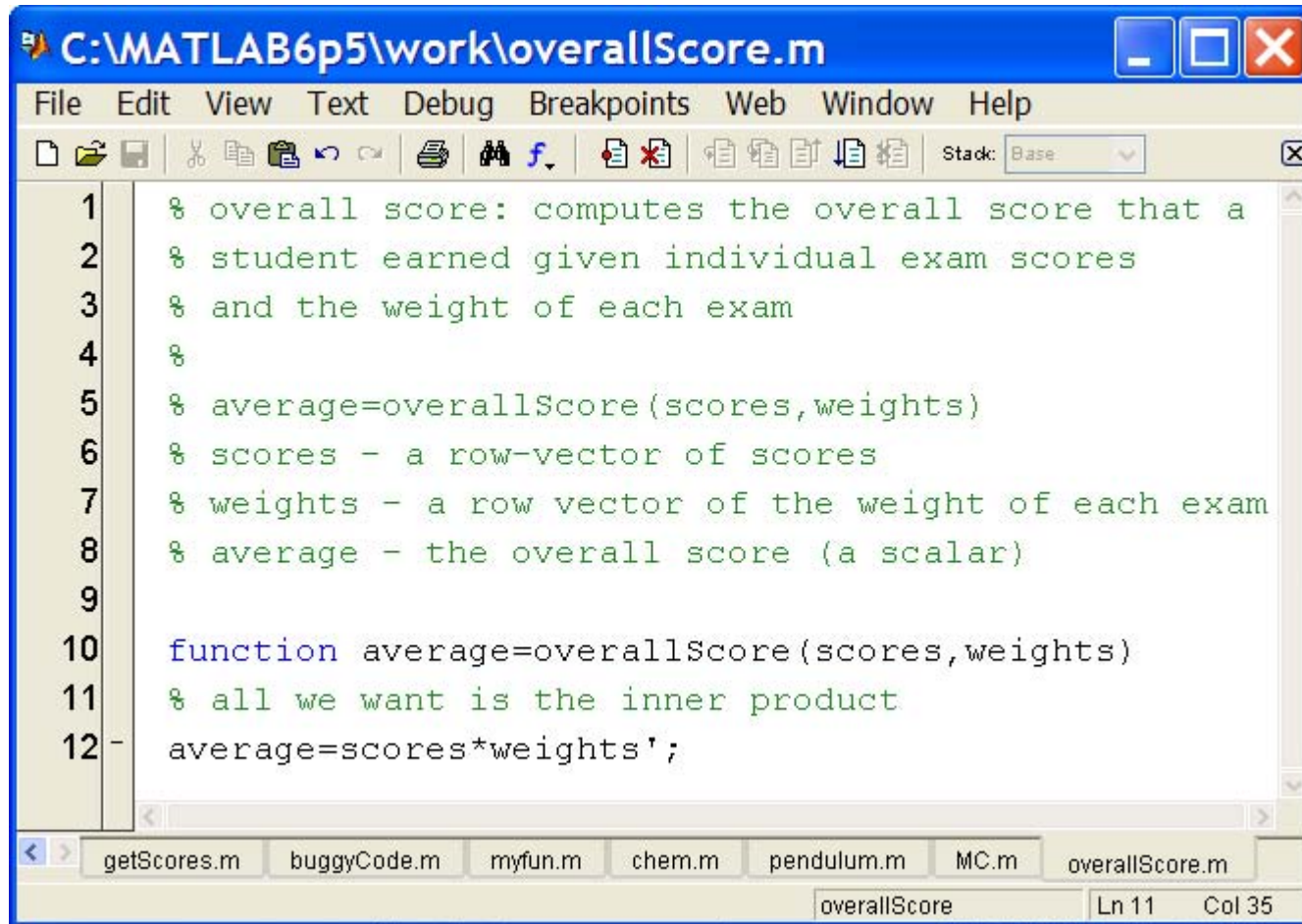


- No need for return:** MATLAB returns the variables whose names match those in the function declaration
- Variable scope:** Any variables created within the function but not returned disappear after the function stops running
- Can have variable input arguments (see **help varargin**)

Functions: Exercise

- Take the script we wrote to calculate the student's overall score and make it into a function
- The inputs should be
 - the scores row vector
 - the weight row vector, with the same length as scores
- The output should be
 - A scalar: the overall score
- Assume the user knows the input constraints (no need to check if the inputs are in the correct format\size)
- Name the function overallScore.m

Functions: Exercise



A screenshot of the MATLAB 6.5 editor window. The title bar reads 'C:\MATLAB6p5\work\overallScore.m'. The menu bar includes File, Edit, View, Text, Debug, Breakpoints, Web, Window, and Help. The toolbar contains icons for file operations, editing, and debugging. The main text area shows the following code:

```
1 % overall score: computes the overall score that a
2 % student earned given individual exam scores
3 % and the weight of each exam
4 %
5 % average=overallScore(scores,weights)
6 % scores - a row-vector of scores
7 % weights - a row vector of the weight of each exam
8 % average - the overall score (a scalar)
9
10 function average=overallScore(scores,weights)
11 % all we want is the inner product
12 average=scores*weights';
```

The status bar at the bottom shows the current file is 'overallScore.m' at line 11, column 35. Other open files in the background include getScores.m, buggyCode.m, myfun.m, chem.m, pendulum.m, and MC.m.

Courtesy of The MathWorks, Inc. Used with permission.

Functions

- We're familiar with
 - » `zeros`
 - » `size`
 - » `length`
 - » `sum`
- Look at the help file for size by typing
 - » `help size`
- The help file describes several ways to invoke the function
 - `D = SIZE(X)`
 - `[M,N] = SIZE(X)`
 - `[M1,M2,M3,...,MN] = SIZE(X)`
 - `M = SIZE(X,DIM)`

Functions

- MATLAB functions are generally overloaded
 - Can take a variable number of inputs
 - Can return a variable number of outputs
- What would the following commands return:
 - » `a=zeros(2,4,8);`
 - » `D=size(a)`
 - » `[m,n]=size(a)`
 - » `[x,y,z]=size(a)`
 - » `m2=size(a,2)`
- Take advantage of overloaded methods to make your code cleaner!

Outline

(1) Plotting Continued

(2) Scripts

(3) Functions

(4) Flow Control

Relational Operators

- MATLAB uses *mostly* standard relational operators
 - equal ==
 - **not** equal ~=
 - greater than >
 - less than <
 - greater or equal >=
 - less or equal <=
- Logical operators

	normal	bitwise
➤ And	&	&&
➤ Or		
➤ Not	~	
➤ Xor	xor	
➤ All true	all	
➤ Any true	any	
- Boolean values: zero is false, nonzero is true
- See **help .** for a detailed list of operators


if/else/elseif

- Basic flow-control, common to all languages
- MATLAB syntax is somewhat unique

IF

```
if cond
    commands
end
```

Conditional statement:
evaluates to true or false



ELSE

```
if cond
    commands1
else
    commands2
end
```

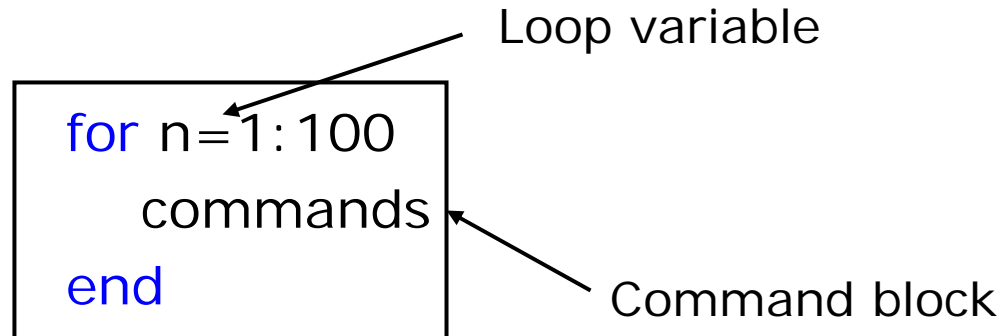
ELSEIF

```
if cond1
    commands1
elseif cond2
    commands2
else
    commands3
end
```

- **No need for parentheses:** command blocks are between reserved words

for

- for loops: use for a definite number of iterations
- MATLAB syntax:



- The loop variable
 - Is defined as a vector
 - Is a scalar within the command block
 - Does not have to have consecutive values
- The command block
 - Anything between the **for** line and the **end**

while

- The while is like a more general for loop:
 - Don't need to know number of iterations

```
      WHILE  
while cond  
  commands  
end
```

- The command block will execute while the conditional expression is true
- Beware of infinite loops!

Exercise: Control-Flow

- Write a function to calculate the factorial of an integer N using a loop (you can use a for or while loop). If the input is less than 0, return NaN. Test it using some values.

```
» function a = factorial(N)
» if N<0,
»     a=nan,
» else
»     a = 1;
»     for k=1:N
»         a = a*k;
»     end
» end
```

- But note that factorial() is already implemented! You should see if there are built-in functions before implementing something yourself.
 - » `which factorial`

find

- **find** is a very important function
 - Returns indices of nonzero values
 - Can simplify code and help avoid loops
- Basic syntax: `index=find(cond)`
 - » `x=rand(1,100);`
 - » `inds = find(x>0.4 & x<0.6);`
- `inds` will contain the indices at which `x` has values between 0.4 and 0.6. This is what happens:
 - `x>0.4` returns a vector with 1 where true and 0 where false
 - `x<0.6` returns a similar vector
 - The `&` combines the two vectors using an and
 - The `find` returns the indices of the 1's

Exercise: Flow Control

- Given $x = \sin(\text{linspace}(0, 10 \cdot \pi, 100))$, how many of the entries are positive?

Using a loop and if/else

```
count=0;
for n=1:length(x)
    if x(n)>0
        count=count+1;
    end
end
```

Being more clever

```
count=length(find(x>0));
```

length(x)	Loop time	Find time
100	0.01	0
10,000	0.1	0
100,000	0.22	0
1,000,000	1.5	0.04

- Avoid loops like the plague!
- Built-in functions will make it faster to write and execute

Efficient Code

- Avoid loops whenever possible
 - This is referred to as vectorization
- Vectorized code is more efficient for MATLAB
- Use indexing and matrix operations to avoid loops
- For example:

```
» a=rand(1,100);
```

```
» b=zeros(1,100);
```

```
» for n=1:100
```

```
»     if n==1
```

```
»         b(n)=a(n);
```

```
»     else
```

```
»         b(n)=a(n-1)+a(n);
```

```
»     end
```

```
» end
```

➤ Slow and complicated

```
» a=rand(1,100);
```

```
» b=[0 a(1:end-1)]+a;
```

➤ Efficient and clean

Exercise: Vectorization

- Alter your factorial program to work WITHOUT a loop. Use **prod**
 - » `function a=factorial(N)`
 - » `a=prod(1:N);`
- You can tic/toc to see how much faster this is than the loop!
- **BUT**...Don't ALWAYS avoid loops
 - Over-vectorizing code can obfuscate it, i.e. you won't be able to understand or debug it later
 - Sometime a loop is the right thing to do, it is clearer and simple

End of Lecture 2

- (1) Plotting Continued
- (2) Scripts
- (3) Functions
- (4) Flow Control

**Vectorization makes
coding fun!**

